



Standard Practice for Life and Reliability Testing Based on the Exponential Distribution¹

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1. Scope

1.1 This practice presents standard sampling procedures and tables for life and reliability testing in procurement, supply, and maintenance quality control operations as well as in research and development activities.

1.2 This practice describes general procedures and definitions of terms used in life test sampling and describes specific procedures and applications of the life test sampling plans for determining conformance to established reliability requirements.

1.3 This practice is an adaptation of the Quality Control and Reliability Handbook H-108, "Sampling Procedures and Tables for Life and Reliability Testing (Based on Exponential Distribution)," U.S. Government Printing Office, April 29, 1960.

1.4 A system of units is not specified in this practice.

1.5 *This standard does not purport to address all of the safety concerns, if any, associated with its use. It is the responsibility of the user of this standard to establish appropriate safety and health practices and determine the applicability of regulatory limitations prior to use.*

2. Referenced Documents

2.1 *ASTM Standards:*²

E 456 Terminology Relating to Quality and Statistics

E 2234 Practice for Sampling a Stream of Product by Attributes Indexed by AQL

E 2555 Practice for Factors and Procedures for Applying the MIL-STD-105 Plans in Life and Reliability Inspection

3. Terminology

3.1 *Definitions*—See Terminology E 456 for a more extensive listing of terms in ASTM Committee E11 standards.

¹ This practice is under the jurisdiction of ASTM Committee E11 on Quality and Statistics and is the direct responsibility of Subcommittee E11.30 on Statistical Quality Control.

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² For referenced ASTM standards, visit the ASTM website, www.astm.org, or contact ASTM Customer Service at service@astm.org. For *Annual Book of ASTM Standards* volume information, refer to the standard's Document Summary page on the ASTM website.

3.1.1 *consumer's risk*, β , n —probability that a lot having specified rejectable quality level will be accepted under a defined sampling plan. **E 2555**

3.1.1.1 *Discussion*—In this practice, the consumer's risk is the probability of accepting lots with mean time to failure θ_1 .

3.1.1.2 *Discussion*—For the procedures of 9.7 and 9.8, the consumer's risk may also be defined as the probability of accepting lots with unacceptable proportion of lot failing before specified time, p_1 .

3.1.2 *life test*, n —process of placing one or more units of product under a specified set of test conditions and measuring the time until failure for each unit.

3.1.3 *mean time to failure*, θ , n —in life testing, the average length of life of items in a lot.

3.1.3.1 *Discussion*—Also known as mean life.

3.1.4 *number of failures*, n —number of failures that have occurred at the time the decision as to lot acceptability is reached.

3.1.4.1 *Discussion*—The expected number of failures required for decision is the average of the number of failures required for decision when life tests are conducted on a large number of samples drawn at random from the same exponential distribution.

3.1.5 *producer's risk*, α , n —probability that a lot having specified acceptable quality level will be rejected under a defined sampling plan.

3.1.5.1 *Discussion*—In this practice, the producer's risk is the probability of rejecting lots with mean time to failure θ_0 .

3.1.5.2 *Discussion*—For the procedures of 9.7 and 9.8, the producer's risk may also be defined as the probability of rejecting lots with acceptable proportion of lot failing before specified time, p_0 .

3.1.6 *sequential life test*, n —life test sampling plan whereby neither the number of failures nor the time required to reach a decision are fixed in advance but instead decisions depend on the accumulated results of the life test.

3.1.7 *unit of product*, n —that which is inspected to determine its classification as defective or nondefective or to count the number of defects. **E 2234**

3.1.8 *waiting time, n—in life testing*, the time elapsed from the start of testing until a decision is reached as to lot acceptability.

3.1.8.1 *Discussion*—The expected waiting time required for decision is the average of the waiting times required for decision when life tests are conducted on a large number of samples drawn at random from the same exponential distribution.

4. Significance and Use

4.1 This practice was prepared to meet a growing need for the use of standard sampling procedures and tables for life and reliability testing in government procurement, supply, and maintenance quality control (QC) operations as well as in research and development activities where applicable.

4.2 A characteristic feature of most life tests is that the observations are ordered in time to failure. If, for example, 20 radio tubes are placed on life test, and t_i denotes the time when the i th tube fails, the data occur in such a way that $t_1 \leq t_2 \leq \dots \leq t_n$. The same kind of ordered observations will occur whether the problem under consideration deals with the life of electric bulbs, the life of electronic components, the life of ball bearings, or the length of life of human beings after they are treated for a disease. The examples just given all involve ordering in time.

4.3 In destructive testing involving such situations as the current needed to blow a fuse, the voltage needed to break down a condenser, or the force needed to rupture a physical material, the test can often be arranged in such a way that every item in the sample is subjected to precisely the same stimulus (current, voltage, or stress). If this is done, then clearly the weakest item will be observed to fail first, the second weakest next, and so forth. While the random variable considered mostly in this guide is time to failure, it should be emphasized, however, that the methodology provided herein can be adapted to the testing situations mentioned above when the random variable is current, voltage, stress, and so forth.

4.4 Sections 6 and 7 describe general procedures and definitions of terms used in life test sampling. Sections 8, 9, and 10 describe specific procedures and applications of the life test sampling plans for determining conformance to established reliability requirements.

4.5 Whenever the methodology or choice of procedures in the practice requires clarification, the user is advised to consult a qualified mathematical statistician, and reference should be made to appropriate technical reports and other publications in the field.

5. Introduction

5.1 The theory underlying the development of the life test sampling plans of this section, including the operating characteristic curves, assumes that the measurements of the length of life are drawn from an exponential distribution. Statistical test procedures for determining the validity of the exponential distribution assumption have appeared in the technical statistical journals. Professor Benjamin Epstein published a comprehensive paper (in two parts) on this subject in the February

and May 1960 issues of *Technometrics*.³ Part I of the paper contains descriptions of the mathematical and graphical procedures as well as an extensive bibliography for reference purposes. Numerical examples illustrating the statistical procedures are included in Part II of the paper.

5.2 It is important to note that the life test sampling plans of this practice are not to be used indiscriminately simply because it is possible to obtain life test data. Only after the exponential assumption is deemed reasonable should the sampling plans be used.

5.3 Sections 6 and 7 describe general procedures and description of life test sampling plans. Section 8 describes specific procedures and applications of sampling plans when life tests are terminated upon the occurrence of a preassigned number of failures, and Section 9 provides sampling plans when life tests are terminated at a preassigned time. Section 10 describes sequential life test sampling plans. Section 8 covers: (1) acceptance procedures; (2) expected duration of life tests and cost considerations in selection of sample sizes; and (3) life test plans for certain specified values of α , β , and θ_1/θ_0 . Section 9 covers: (1) acceptance procedures; (2) life test plans for certain specified values of α , β , θ_1/θ_0 , and T/θ_0 ; and (3) life test plans based on proportion of lot failing before specified time. Section 10 covers: (1) acceptance procedures; (2) graphical acceptance procedures; and (3) expected number and waiting time required for decision.

5.4 Operating characteristic (OC) curves for the life test sampling plans of 8.1-8.5, 9.1-9.5, and Section 10 are shown in Fig. A1.1 for the corresponding sampling plans in these sections were matched with respect to their OC curves. The OC curves in Fig. A1.1 have been computed for the life test sampling plans of 8.1-8.5 but are equally applicable for the sampling plans of 9.1-9.5 and Section 10.

5.5 The procedures of this section are based on the premise that the life tests are monitored continuously. If the tests are monitored only periodically, the values obtained from the tables and curves are only approximations.

6. General Definitions of Life and Reliability Test Terms

6.1 Discussion of Terms and Procedures:

6.1.1 *Purpose*—This section provides definitions of terms required for the life test sampling plans and procedures of Sections 7 through 10.

6.1.2 *Life Test*—Life test is the process of placing the “unit of product” under a specified set of test conditions and measuring the time it takes until failure.

6.1.3 *Unit of Product*—The unit of product is the entity of product that may be placed on life test.

6.1.4 *Specifying Failure*—The state that constitutes a failure shall be specified in advance of the life test.

6.1.5 *Life Test Sampling Plan*—A life test sampling plan is a procedure that specifies the number of units of product from a lot that are to be tested and the criterion for determining acceptability of the lot.

³ Epstein, B., “Tests for the Validity of the Assumption that the Underlying Distribution of Life is Exponential,” *Technometrics*, Vol 2, Feb 1960 and May 1960, pp. 83-101 and 167-183.

6.1.6 Life Test Terminated upon Occurrence of Preassigned Number of Failures—Life test sampling plans whereby testing is terminated when a preassigned termination number of failures, r , occur are given in Section 8 of this practice.

6.1.7 Life Test Terminated at Preassigned Time—Life test sampling plans whereby testing is terminated when a preassigned termination time, T , is reached are given in Section 9 of this practice.

6.1.8 Sequential Life Test—Sequential life test is a life test sampling plan whereby neither the number of failures nor the time required to reach a decision are fixed in advance but, instead, decisions depend on the accumulated results of the life test. Information on the observed time to failure are accumulated over time and the results at any time determine the choice of one among three possible decisions: (1) the lot meets the acceptability criterion, (2) the lot does not meet the acceptability criterion, or (3) the evidence is insufficient for either decision (1) or (2) and the test must continue. Sequential life test sampling plans are given in Section 10 of this practice and have the advantage over the life test sampling plans mentioned in 6.1.6 and 6.1.7 in that, for the same OC curve, the expected waiting time and the expected number of failures required to reach a decision as to lot acceptability are less for the sequential life tests.

6.1.9 Expected Number of Failures—The number of failures required for decision is the number of failures that have occurred at the time the decision as to lot acceptability is reached. For the life test sampling plans mentioned in 6.1.6, this number of failures is known in advance of the life test; but, for the sampling plans mentioned in 6.1.7 and 6.1.8, this number cannot be predetermined. The expected number of failures required for decision is the average of the number of failures required for decision when life tests are conducted on a large number of samples drawn at random from the same exponential distribution. The expected number of failures can be predetermined for the sampling plans mentioned in 6.1.6-6.1.8.

6.1.10 Expected Waiting Time—The waiting time required for decision is the time elapsed from the start of the life test to the time decision is reached as to lot acceptability. The waiting time required for decision cannot be predetermined for any of the sampling plans mentioned in 6.1.6-6.1.8. The expected waiting time required for decision is the average of the waiting times required for decision when life tests are conducted on a large number of samples drawn at random from the same exponential distribution. The expected waiting time can be predetermined for the sampling plans mentioned in 6.1.6-6.1.8.

6.2 Length of Life:

6.2.1 Length of Life—The terms “length of life” and “time to failure” may be used interchangeably and shall denote the length of time it takes for a unit of product to fail after being placed on life test. The length of time may be expressed in any convenient time scale such as seconds, hours, days, and so forth.

6.2.2 Mean Time to Failure—The terms “mean time to failure” and “mean life” may be used interchangeably and shall denote the mean (or equivalently, the average) length of life of items in the lot. Mean life is denoted by θ .

6.2.3 Acceptable Mean Life—The acceptable mean life, θ_0 , is the minimum mean time to failure that is considered satisfactory.

6.2.4 Unacceptable Mean Life—The unacceptable mean life, θ_1 ($\theta_1 < \theta_0$), is the mean time to failure such that lots having a mean life less than or equal to θ_1 are considered unsatisfactory. The interval between θ_0 and θ_1 is a zone of indifference in which there is a progressively greater degree of dissatisfaction as the mean life decreases from θ_0 to θ_1 .

6.3 Failure Rate:

6.3.1 Proportion of Lot Failing Before Specified Time—The term “proportion of lot failing before specified time,” p , denotes the fraction of the lot that fails before some specified time, T , that is:

$$p = 1 - \exp(-T/\theta) \quad (1)$$

6.3.2 Failure Rate during Period of Time—The “failure rate during period of time T ,” G , is given by:

$$G = \frac{1}{T} \{1 - \exp(T/\theta)\} = p/T \quad (2)$$

6.3.3 Instantaneous Failure Rate—The “instantaneous failure rate” or “hazard rate” is given by:

$$Z = 1/\theta \quad (3)$$

6.3.4 Acceptable Proportion of Lot Failing Before Specified Time—The “acceptable proportion of lot failing before specified time,” p_0 , is the maximum fraction of the lot that may fail before time, T , and still result in the lot being considered satisfactory.

6.3.5 Unacceptable Proportion of Lot Failing Before Specified Time—The “unacceptable proportion of lot failing before specified time,” p_1 , ($p_1 > p_0$), is the minimum fraction of the lot that may fail before time, T , and results in the lot being considered unsatisfactory. The interval between p_0 and p_1 is a zone of indifference in which there is a progressively greater degree of dissatisfaction as the fraction of the lot failing before time, T , increases from p_0 to p_1 .

6.3.6 Acceptable Failure Rate During Period of Time—The “acceptable failure rate during period of time,” G_0 , is the maximum failure rate during the period of time that can be considered satisfactory.

6.3.7 Unacceptable Failure Rate During Period of Time—The “unacceptable failure rate during period of time,” G_1 , ($G_1 > G_0$), is the minimum failure rate during the period of time that results in the lot being considered unsatisfactory. The interval between G_0 and G_1 is a zone of indifference in which there is a progressively greater degree of dissatisfaction as the failure rate increases from G_0 to G_1 .

6.3.8 Life Test Sampling Plans Based on Failure Rates—Life test sampling plans that are based on failure rates are given in 9.7 and 9.8.

6.4 OC Curves and Sampling Risks:

6.4.1 OC Curve—The OC curve of a life test sampling plan is the curve that shows the probability that a submitted lot with given mean life would meet the acceptability criterion on the basis of that sampling plan.

6.4.2 Producer’s Risk—The producer’s risk, α , is the probability of rejecting lots with mean life, θ_0 . For the procedures of 9.7 and 9.8, the producer’s risk may also be defined as the

probability of rejecting lots with acceptable proportion of lot failing before specified time, p_0 .

6.4.3 Consumer's Risk—The consumer's risk, β , is the probability of accepting lots with mean life, θ_1 . For the procedures of 9.7 and 9.8, the consumer's risk may also be defined as the probability of accepting lots with p_1 as the unacceptable proportion of lot failing before specified time.

6.5 Submittal of Product:

6.5.1 Lot—The term "lot" shall mean either an "inspection lot," that is, a collection of units of product manufactured under essentially the same conditions from which a sample is drawn and tested to determine compliance with the acceptability criterion or, a "preproduction lot," that is, one or more units of product submitted before the initiation of production for test to determine compliance with the acceptability criterion.

6.6 Sample Selection:

6.6.1 Drawing of Samples—A sample is one or more units of product drawn at random from a lot.

6.6.2 Testing without Replacement—Life test sampling without replacement is a life test procedure whereby failed units are not replaced.

6.6.3 Testing with Replacement—Life test sampling with replacement is a life test procedure whereby the life test is continued with each failed unit of product replaced by a new one, drawn at random from the same lot, as soon as the failure occurred. In the case of complex unit of product, this may be interpreted to mean replacement of the component that caused the failure by a new component drawn at random from the same lot of components. When the "sample sizes" are the same in both instances, the expected waiting time required for decision when testing with replacement is less than when testing without replacement.

6.6.4 Sample Size—The sample size, n , for a life test is the number of units of product placed on test at the start of a life test. When testing with replacement, the total number of units of product placed on test will, in general, be greater than the original sample size. The sample sizes for the life test plans of Sections 8 to 10 depend on the relative cost of placing large numbers of units of product on test and the expected length of time the life tests must continue to determine acceptability of the lots. Increasing the sample size will, on one hand, cut the average time required to determine acceptability but, on the other hand, will increase the cost because of placing more units of product on test.

6.7 Exponential Distribution:

6.7.1 Exponential Distribution with One Parameter—The density function for the exponential distribution with one parameter is given by:

$$f(t; \theta) = 1/\theta \exp(-t/\theta) \quad t \geq 0, \theta > 0 \quad (4)$$

$$= 0 \quad t < 0$$

6.7.1.1 The function has the following general graphical form:

6.7.2 Exponential Distribution with Two Parameters—The density function for the exponential distribution with two parameters is given by:

$$f(t; \theta, A) = 1/\theta \exp[-(t - A)/\theta] \quad t \geq A \geq 0 \quad (5)$$

$$= 0 \quad \text{elsewhere}$$

6.7.2.1 The function has the following general graphical form:

6.7.2.2 The quantity, A , is called "guarantee time" and the one parameter case is a special case of the two-parameter distribution with a guarantee time of zero.

6.7.3 Exponential Distribution when Number of Parameters Is Unspecified—In this practice, whenever the term "exponential distribution" is mentioned without specific mention of the number of parameters, it shall be assumed to mean the exponential distribution with one parameter.

7. General Description of Life Test Sampling Plans

7.1 Scope:

7.1.1 Purpose—Sections 7 through 10 of this practice establish life test sampling plans for determining acceptability of a product when samples are drawn at random from an exponential distribution.

7.1.2 Specifying Acceptable Mean Life—Before the start of the life test, the particular value of the acceptable mean life, θ_0 , shall be specified except when using the procedures of 9.7 and 9.8.

7.1.3 Specifying Unacceptable Mean Life—The particular value of the unacceptable mean life, θ_1 , shall be specified in advance of the life test when using the life test procedures of 8.6 and 9.6.

7.1.4 Specifying Acceptable Proportion of Lot Failing before Specified Time—The particular value, p_0 , of the acceptable proportion of lot failing before specified time to be used in the life test shall be specified in advance for the procedures of 9.7 and 9.8.

7.1.5 Specifying Unacceptable Proportion of Lot Failing before Specified Time—The particular value, p_1 , of the unacceptable proportion of lot failing before specified time shall be specified in advance of the life test when using the procedures of 9.7 and 9.8.

7.2 Sampling Risks:

7.2.1 Producer's Risk—The producer's risk, α , is the probability of rejecting lots with mean life, θ_0 . For the procedures of 9.7 and 9.8, the producer's risk may also be defined as the probability of rejecting lots with p_0 as the acceptable proportion of lot failing before specified time. Summarized in the following are the various numerical values of α and the master sampling tables in which they are given.

Procedures for	Producer's Risk	Table
8.1-8.5	0.01, 0.05, 0.10, 0.25, 0.50	Table A1.2
8.6	0.01, 0.05, 0.10, 0.25	Table A1.7
9.1-9.5	0.01, 0.05, 0.10, 0.25, 0.50	Tables A1.8-A1.12 and Tables A1.13-A1.17
9.6	0.01, 0.05, 0.10, 0.25	Table A1.18 and Table A1.19
9.7 and 9.8	0.01, 0.05, 0.10	Table A1.20
10	0.01, 0.05, 0.10, 0.25, 0.50	Tables A1.21-A1.25

7.2.2 Specifying Producer's Risk—The particular value of α to be used in the life test shall be selected from among those given in 7.2.1 and specified in advance of the life test.

7.2.3 Consumer's Risk—The consumer's risk, β , is the probability of accepting lots with mean life, θ_1 . For the procedures of 9.7 and 9.8, the consumer's risk may also be defined as the probability of accepting lots with p_1 as the unacceptable proportion of lot failing before specified time. Summarized in the following are the various numerical values of β and the master sampling tables in which they are given.

Procedures for	Consumer's Risk	Table
8.1-8.5	0.10	Table A1.2
8.6	0.01, 0.05, 0.10, 0.25	Table A1.7
9.1-9.5	0.10	Tables A1.8-A1.12 and Tables A1.13-A1.17
9.6	0.01, 0.05, 0.10, 0.25	Table A1.18 and Table A1.19
9.7 and 9.8	0.01, 0.05, 0.10	Table A1.20
10	0.10	Tables A1.21-A1.25

7.2.3.1 The smaller the value of β , the greater is the protection against acceptance of lots with low mean life or high failure rate.

7.2.4 Specifying Consumer's Risk—The particular value of β to be used in the life test shall be selected from among those given in 7.2.3 and specified in advance of the life test.

7.3 OC Curves:

7.3.1 OC Curve—The OC curve of a life test sampling plan is the curve that shows the probability that a submitted lot with given mean life would meet the acceptability criterion on the basis of that sampling plan. The OC curves given in Fig. A1.1 are equally applicable for the sampling plans of 8.1-8.5, 9.1-9.5, and Section 10. Moreover, the OC curves are also equally applicable for both the sampling with and without replacement procedures. The abscissas of the OC curves are expressed as the ratio θ/θ_0 in Fig. A1.1 so that the same set of OC curves is applicable regardless of the value of the specified acceptable mean life θ_0 .

7.3.2 Sampling Plan Code Designation—The life test sampling plans of 8.1-8.5, 9.1-9.5, and Section 10, along with their associated OC curves, are designated by code letters and numbers. The sample code is given in Table A1.1 and is determined by the values of α , β , and θ_1/θ_0 . The OC curves of all sampling plans designated by the same code pass through the two points (1, $1-\alpha$) and (θ_1/θ_0 , $\beta = 0.10$). Thus, all sampling plans that are designated by the same code offer essentially the same protection.

7.3.3 Ratio θ_1/θ_0 as Measure of Protection Offered by Sampling Plan—The consumer's risk β has been defined in 7.2.3 as the risk of accepting lots with mean life, θ_1 . Because the OC curves are drawn with abscissa, θ_1/θ_0 , the ratio, θ_1/θ_0 , is also a measure of mean life that is accepted with probability, β . The ratio, θ_1/θ_0 , shall be greater than zero but less than unity. If α , β , and θ_0 are kept constant, as θ_1/θ_0 increases, the protection offered by the sampling plan against accepting lots with low mean life also increases. Thus, Table A1.1 allows comparisons in the amount of protection offered by the various sampling plans, for in any column, the protection increases as θ_1/θ_0 increases.

7.4 Specifying Acceptance Procedures—To identify completely the sampling plan to be used, the following shall be specified for the sampling plans of:

8.1-8.5	α , r , θ_0 or sample plan code, θ_0
8.6	α , β , θ_0 , θ_1
9.1-9.5	θ_0 , r , α , n or sample plan code, n , θ_0
9.6	α , β , θ_0 , θ_1 , T
9.7 and 9.8	α , β , p_0 , p_1 , T or α , β , G_0 , G_1 , T
10	Sample plan code, θ_0

7.4.1 In addition, the use of life testing with or without replacement may be specified, except when using the sampling plans of 9.7 and 9.8.

8. Life Tests Terminated upon Occurrence of Preassigned Number of Failures

8.1 Life Test Sampling Plans—This part of the practice describes the procedures for use with life tests that are terminated upon the occurrence of a preassigned number of failures. Two procedures are given: (1) a procedure when testing without replacement and (2) another procedure when testing with replacement.

8.1.1 Use of Life Test Sampling Plans—To determine whether the lot meets the acceptability criterion with respect to average length of life, the applicable sampling plan shall be used in accordance with the provisions of Section 7 and those in this part of the practice.

8.1.2 Drawing of Samples—All samples shall be drawn in accordance with 6.6.

8.2 Selecting the Life Test Sampling Plan:

8.2.1 Master Sampling Table—The master sampling table for the life test sampling plans of this part of the practice is Table A1.2.

8.2.2 Obtaining the Sampling Plan—The life test sampling plan consists of a sample size, a termination number, and an associated acceptability constant. The sampling plan is obtained from Master Table A1.2.

8.2.2.1 Sample Sizes—For the procedures of 8.1-8.5, the acceptability constants and the OC curves do not depend on the number of units of product placed on test. The sample size, as mentioned in 6.6.4, depends on the relative cost of placing large numbers of units of product on test and the expected length of time the life test shall continue. The sample size may be selected by using the procedures of 8.5.

8.2.2.2 Termination Number—The termination number, r , may be selected from among those given in Table A1.2 and specified before the initiation of the life test. The choice of this number shall be dependent on the degree of protection desired against acceptance of material with unacceptable mean life. The larger the termination number, the larger is the ratio, θ_1/θ_0 , and, as mentioned in 7.3.3, the greater is the assurance against accepting material with an unacceptable mean life.

8.2.2.3 Acceptability Constant—The acceptability constant, C , corresponding to the applicable termination number, r , and producer's risk, α , is obtained from the master table by multiplying the tabled entry by the acceptable mean life, θ_0 .

8.3 Lot Acceptability Procedures when Testing without Replacement:

8.3.1 Estimate of Mean Life—The acceptability of a lot, when using a life test from this part of the practice, shall be judged by the quantity, $\hat{\theta}_{r,n}$.

8.3.2 Computation—The following quantity shall be computed from the test results:

$$\hat{\theta}_{r,n} = \frac{1}{r} \left[\sum_{i=1}^r x_{i,n} + (n-r)x_{r,n} \right] \quad (6)$$

where:

$\hat{\theta}_{r,n}$ = estimate of the lot mean life,

r = termination number,

n = sample size, and

$x_{i,n}$ = time when the i th failure occurs. $i = 1, 2, \dots, r$.

8.3.3 Acceptability Criterion—Compare the quantity $\hat{\theta}_{r,n}$ with the acceptability constant C , mentioned in 8.2.2.3. If $\hat{\theta}_{r,n}$ is equal to or greater than C , the lot meets the acceptability criterion; if $\hat{\theta}_{r,n}$ is less than C , then the lot does not meet the acceptability criterion.

8.4 Lot Acceptability Procedures when Testing With Replacement:

8.4.1 Estimate of Mean Life—The acceptability of a lot, when using a life test from this part of the practice, shall be judged by the quantity $\hat{\theta}_{r,n}$.

8.4.2 Computation—The following quantity shall be computed from the test results:

$$\hat{\theta}_{r,n} = n x_{r,n} / r \quad (7)$$

where:

$\hat{\theta}_{r,n}$ = estimate of the lot mean life,

r = termination number,

n = original sample size, and

$x_{r,n}$ = time when the r th failure occurs.

8.4.3 Acceptability Criterion—Compare the quantity $\hat{\theta}_{r,n}$ with the acceptability constant, C , mentioned in 8.2.2.3. If $\hat{\theta}_{r,n}$ is equal to or greater than C , the lot meets the acceptability criterion; if $\hat{\theta}_{r,n}$ is less than C , then the lot does not meet the acceptability criterion.

8.4.3.1 Example 1: Use of Table A1.2—Find a life test plan that is to be stopped on the occurrence of the fifth failure and will accept a lot having an acceptable mean life of 1000 h with probability 0.90.

8.4.3.2 Solution—In the notation of this section, $\theta_0 = 1000$, $\alpha = 0.10$, and $r = 5$. In the testing without replacement case:

$$\hat{\theta}_{r,n} = \frac{1}{5} [x_{1,n} + x_{2,n} + x_{3,n} + x_{4,n} + x_{5,n} + (n-5)x_{5,n}] \quad (8)$$

(1) In the replacement case, $\hat{\theta}_{r,n} = n x_{5,n} / 5$. The acceptability criterion is, accept the lot if:

$$\begin{aligned} \hat{\theta}_{5,n} &\geq C \\ &\geq \theta_0(C/\theta_0) = (1000)(0.487) = 487 \end{aligned} \quad (9)$$

(2) The quantity $C/\theta_0 = 0.487$ is obtained from Table A1.2. In words, place n items on test. Wait until the first five failures occur. Compute $\hat{\theta}_{5,n}$. Accept the lot if $\hat{\theta}_{5,n} \geq 487$; reject the lot otherwise.

(3) The code designation for the above life test sampling plan is obtained from Table A1.2 as C-5. From Fig. A1.1, the probability of accepting a lot with mean life of, say, 500 h may be obtained by finding the ordinate of the OC curve labeled C-5 at the point where the abscissa $\theta/\theta_0 = 500/1000 = 0.5$. The probability is seen to be equal to 0.47.

(4) In this example, if the termination number had been selected as 6 instead of 5, the probability of accepting a lot with mean life of 500 h is obtained from the OC curve labeled C-6. The probability is seen to equal 0.41. This illustrates the remark made in 8.2.2.2 that the larger the termination number, the higher the probability of rejecting lots with unacceptable mean life.

8.4.3.3 Example 2: Calculations for Testing Without Replacement—Suppose that in the life test of Example 1, 10 units of product had been placed on test. If the failed units were not replaced and the first 5 failure times were 50, 75, 125, 250, and 300, determine whether the lot met the acceptability criterion.

8.4.3.4 Solution—In this case:

$$\hat{\theta}_{5,10} = \frac{50 + 75 + 125 + 250 + 300 + 5(300)}{5} = 460 \quad (10)$$

(1) Since $460 < 487$, the lot did not meet the acceptability criterion.

8.4.3.5 Example 3: Calculations for Testing With Replacement—Suppose that in the life test of Example 1, 10 units of product had been placed on test. If the failed units were replaced immediately and the first 5 failure times were 56, 128, 176, 276, and 442, determine whether the lot met the acceptability criterion.

8.4.3.6 Solution—In this case:

$$\hat{\theta}_{5,10} = \frac{10(442)}{5} = 884 \quad (11)$$

(1) Since $884 > 487$, the lot met the acceptability criterion.

8.5 Expected Waiting Time of Life Tests and Cost Considerations in Selection of Sample Sizes—The operating characteristics of the life test sampling plans of 8.1-8.4 are independent of the number of units of product placed on test. Thus, all tests based on common values of the termination number, r , and producer's risk, α , are equally good, and the choice of the sample size, n , depends only on the relative cost of placing a large number of units of product on test and the expected waiting time required for decision. For fixed α and r , increasing n will, on one hand, cut the expected waiting time; but will, on the other hand, increase the cost because of placing more units of product on test. This part of the practice provides procedures for determining the optimum sample size based on considerations of cost.

8.5.1 Expected Waiting Time—The mean life of the lot and, as noted in 8.5, the size of the sample drawn from the lot affect the expected waiting time required to observe the r th failure in a sample of size n . The r th failure is expected to occur more quickly in samples drawn from lots with low values of mean life. The values of the expected waiting time divided by the mean life of the lot, when testing without replacement, are given in Table A1.3 and Table A1.4. Corresponding values for the testing with replacement situation are not tabled but may be calculated by dividing the termination number, r , by the sample size, n , that is:

$$\frac{\text{Expected Waiting Time}}{\text{Mean Life of a Lot}} = \frac{r}{n} \quad (12)$$

8.5.2 Relative Saving in Time by Increasing Sample Size When Testing Without Replacement—When testing without

replacement, the expected waiting time required to observe the r th failure in a sample of size n , ($n \geq r$), may be obtained from [Table A1.3](#) or [Table A1.4](#) by multiplying the tabled entry by the mean life of the lot. By dividing the expected waiting time when n units of product are placed on test by that when only r units are placed on test, the mean life of the lot cancels out and the ratio

$$\frac{\text{Expected Waiting Time for } r \text{ Failures in Sample of } n}{\text{Expected Waiting Time for } r \text{ Failures in Sample of } r} \quad (13)$$

is a measure of the relative expected saving in time as a result of placing more units of product on test. A brief table of these ratios is given in [Table A1.5](#).

8.5.3 Relative Saving in Time by Increasing Sample Size When Testing With Replacement—When testing with replacement, the expected waiting time required to observe the r th failure in a sample of size n is equal to the quantity $r\theta/n$. By dividing the expected waiting time when n units of product are placed on test by that when only r units are placed on test, the mean life of the lot cancels out and the ratio

$$\text{Relative Saving} = r\theta/n\theta = r/n \quad (14)$$

is a measure of the relative expected saving in time as a result of using larger sample sizes.

8.5.4 Relative Saving in Time by Testing with Replacement as Compared to Testing Without Replacement—When testing with replacement, the expected waiting time required to observe the r th failure in a sample of size n ($n \geq r$) is equal to the quantity $r\theta/n$. When testing without replacement, this expected waiting time may be obtained from [Table A1.3](#) or [Table A1.4](#) by multiplying the tabled entry by the mean life of the lot θ . By dividing these two expected waiting times, the mean life of the lot cancels out and the ratio

$$\frac{\text{Expected Waiting Time for } r \text{ Failures in Sample of } n \text{ When Testing With Replacement}}{\text{Expected Waiting Time for } r \text{ Failures in Sample of } n \text{ When Testing Without Replacement}} \quad (15)$$

is a measure of the relative expected saving in time as a result of sampling with replacement. A brief table of these ratios is given in [Table A1.6](#).

8.5.4.1 Example 4: Saving in Time by Increasing Sample Size When Testing Without Replacement—Compare the average length of time needed to observe the failure of the first two out of five units of product under test with the average length of time required to observe the failure of two out of two units when testing without replacement.

8.5.4.2 Solution—From [Table A1.3](#), it is seen that for $r = 2$ and $n = 2$, the expected waiting time is 1.50000 and that for $r = 2$ and $n = 5$, the expected waiting time is 0.45000. Thus, the relative saving in time by placing five units on test is $0.45000/1.5000 = 0.300$. This figure may also be obtained directly from [Table A1.5](#). Hence, the average time required when five units are placed on test is 30 % of the average time required when only two units are used.

8.5.4.3 Example 5: Saving in Time by Increasing Sample Size When Testing With Replacement—Make the same comparison as in Example 4 ([8.5.4.1](#)) if the testing had been with replacement.

8.5.4.4 Solution—For $r = 2$ and $n = 2$, the expected waiting time is θ and that for $r = 2$ and $n = 5$ is $r\theta/n = 2\theta/5 = 0.4\theta$. Thus, the relative saving in time by placing five units on test is

$0.4\theta/\theta = 0.4$. Hence, the average time required when five units are placed on test is 40 % of the average time required when only two units are used.

8.5.4.5 Example 6: Saving in Time by Testing With Replacement—Compare the average length of time needed to observe the failure of the first five out of five units of product under test when testing with replacement with the average length of time needed when testing without replacement.

8.5.4.6 Solution—When testing with replacement, for $r = 5$ and $n = 5$, the expected waiting time is θ . When testing without replacement, [Table A1.3](#) or [Table A1.4](#) shows that the expected waiting time is 2.28330. Thus, the relative saving in time by testing with replacement is $\theta/2.28330 = 0.438$; or the average time required for a decision, by replacing failed units, is 43.8 % of the average time required when failed units are not replaced. This figure may also be obtained directly from [Table A1.6](#).

8.5.5 Cost Considerations in Choice of Sample Size—Methods for finding the optimum sample size based on considerations of cost are given in this section.

8.5.5.1 Cost When Testing Without Replacement—The total expected cost of any of the life test plans of [8.2](#) when testing without replacement is given by:

$$c_1\theta_0 = \left(\frac{1}{n} + \frac{1}{n-1} + \dots + \frac{1}{n-r+1}\right) + c_2n \quad (16)$$

where:

- c_1 = cost of waiting per unit time,
- c_2 = cost of placing a unit of product on test,
- θ_0 = acceptable mean life,
- r = termination number, and
- n = sample size.

8.5.5.2 Optimum Sample Size When Testing Without Replacement—The value of n , which minimizes the total cost, as determined by the method of [8.5.5.1](#), is the optimum sample size. A general method of obtaining the optimum n is to use [Table A1.3](#) or [Table A1.4](#). The smallest n is chosen such that the difference between the expected waiting time for the r th failure when that number of units of product are placed on test and that when $n + 1$ units are placed on test is less than the quantity $c_2/c_1\theta_0$.

(1) Example 7: Calculation of Costs—Consider the case in which $r = 10$, $\theta_0 = 1000$ h, $c_1 = \$1$ per hour, and $c_2 = \$100$ per unit of product tested. Using the total cost formula, determine the optimum sample size if failed units are not replaced.

(2) Solution—Using the formula of [8.5.5.1](#), the costs for various values of n are:

n	Expected Cost Because of Waiting	Cost of Units Tested	Total Cost
10	2929	1000	3929
11	2020	1100	3120
12	1603	1200	2803
13	1346	1300	2646
14	1168	1400	2568
15	1035	1500	2535
16	931	1600	2531
17	847	1700	2547

(a) The optimum sample size is thus $n = 16$.

(3) Example 8: Obtaining Optimum Sample Size With Expected Waiting Time—Use [Table A1.3](#) to determine the optimum sample size for the problem of Example 7, [8.5.5.2\(1\)](#).

(4) *Solution*—The quantity $c_2/c_1\theta_0$ is equal to 0.1 and, from Table A1.3, the expected waiting times are:

n	Expected Waiting Time to Observe 10th Failure		
	in n	in $n + 1$	Difference
10	2.9290	2.0199	0.9091
11	2.0199	1.6032	0.4167
12	1.6032	1.3468	0.2564
13	1.3468	1.1682	0.1786
14	1.1682	1.0349	0.1333
15	1.0349	0.9307	0.1042
16	0.9307	0.8467	0.0840 ^A
17	0.8467	0.7773	0.0694

^A The optimum sample size is $n = 16$, as was seen in Example 7 (8.5.5.2(1)), since that is the smallest sample size for which the difference in expected waiting times is less than $c_2/c_1\theta_0$ or 0.1.

8.5.5.3 *Cost When Testing With Replacement*—The total expected cost of any of the life test plans of 8.2, when testing with replacement, is given by:

$$c_1\theta_0\frac{r}{n} + c_2(n + r - 1) \quad (17)$$

where:

- c_1 = cost of waiting per unit time,
- c_2 = cost of placing a unit of product on test,
- θ_0 = acceptable mean life,
- r = termination number, and
- n = sample size.

8.5.5.4 *Optimum Sample Size When Testing With Replacement*—The value of n , which minimizes the total cost, as determined by the method of 8.5.5.3, is the optimum sample size. In general, the optimum n for the case of testing with replacement is the integer nearest to:

$$\sqrt{\frac{c_1\theta_0r}{c_2} + \frac{1}{4}} \quad (18)$$

(1) *Example 9: Calculation of Cost*—Consider the problem of Example 7 (8.5.5.2(1)), that is, $r = 10$, $\theta_0 = 1000$, $c_1 = \$1$, and $c_2 = \$100$. Using the total cost formula, determine the optimum sample size if failed units were replaced.

(2) *Solution*—Using the formula of 8.5.5.3, the costs for various values of n , are:

n	Expected Cost	Cost of Units	Total Cost
	Because of Waiting	Tested	
9	1111	1800	2911
10	1000	1900	2900
11	909	2000	2909

(a) The optimum sample size is thus $n = 10$.

(3) *Example 10: Obtaining Optimum Sample Size by Formula*—Use the method of 8.5.5.4 to determine the optimum sample size for the problem of Example 9.

(4) *Solution*—The integer nearest to

$$\sqrt{\frac{1(1000)(10)}{100} + \frac{1}{4}} = 10.012 \quad (19)$$

is 10. This is the optimum sample size as was seen in Example 9 (8.5.5.4(1)).

8.6 *Life Test Sampling Plans for Certain Specified Values of α , β , and θ_1/θ_0* —A life test sampling plan may be designed so that its OC curve meets the following prescribed conditions: if $\theta = \theta_0$, then the probability of the lot meeting the acceptability criterion is less than or equal to β . This part of the practice, which may be considered an extension of 8.1-8.5, provides procedures for obtaining values of the termination number, r ,

and the acceptability constant, C , when certain selected values of α , β , and θ_1/θ_0 are specified. When other values of α , β , and θ_1/θ_0 than those provided in this part of the practice are needed, refer to 8.1-8.5 to determine whether one of the life test sampling plans given in those paragraphs are applicable.

8.6.1 *Life Test Sampling Plans*—From Table A1.7, values of the termination number, r , and the acceptability constant, C , may be obtained for values of $\alpha = 0.01, 0.05, 0.10$, and 0.25 ; $\beta = 0.01, 0.05, 0.10$, and 0.25 ; and $\theta_1/\theta_0 = 2/3, 1/2, 1/3, 1/5$, and $1/10$. The value of r is obtained directly from Table A1.7, but the acceptability constant, C , is obtained by multiplying the tabled entry by the acceptable mean life, θ_0 .

8.6.1.1 *Example 11*—Find a life test sampling plan that possesses the following OC curve: If the mean life is $\theta_0 = 900$ h, the lot is accepted with probability 0.95; if the mean life is $\theta_1 = 300$ h, it is accepted with probability approximately equal to 0.10.

8.6.1.2 *Solution*—In this example, $\theta_1/\theta_0 = 1/3$, $\alpha = 0.05$, and $\beta = 0.10$. Looking in Table A1.7, the termination number $r = 8$ and the acceptability constant $C = \theta_0(C/\theta_0) = 900(0.498) = 448$ are obtained. In word form, place eight or more units of product on test. Stop life testing after eight failures have occurred. If the estimate of lot mean life $\hat{\theta}_{8n}$ is greater than or equal to 448, the lot is acceptable; otherwise, the lot is not acceptable.

8.6.2 *Expansion of Table A1.7 for Values of θ_1/θ_0 Greater Than 2/3*—Approximate values of the termination number, r , and the acceptability constant, C , may be obtained to supplement those given in Table A1.7 for values of θ_1/θ_0 greater than 2/3 provided the same values of α and β as given in Table A1.7 are specified. Compute:

$$r = \left(\frac{K_\beta + (\theta_0/\theta_1)K_\alpha}{(\theta_0/\theta_1) - 1} \right)^2 \quad (20)$$

and

$$C = \theta_0 \left(1 - \frac{K_\alpha}{\sqrt{r}} \right) \quad (21)$$

where values of K_α and K_β are tabulated in the following:

α or β	K_α or K_β ^A
0.01	2.326
0.05	1.645
0.10	1.282
0.25	0.674

^A Value obtained from tables of the cumulative normal distribution.

8.6.2.1 *Example 12*—Find the appropriate values of the termination number, r , and the acceptability constant, C , for the case in which the acceptable mean life, $\theta_0 = 110$ h, the unacceptable mean life, $\theta_1 = 100$ h, the producer's risk, $\alpha = 0.05$, and the consumer's risk, $\beta = 0.10$.

8.6.2.2 *Solution*—From the formulas of 8.6.2:

$$r = \left(\frac{1.282 + (1.1)(1.645)}{0.1} \right)^2 = 956 \quad (22)$$

and

$$C = 110 \left(1 - \frac{1.645}{\sqrt{956}} \right) = 104.15 \quad (23)$$

9. Life Tests Terminated at Preassigned Time

9.1 Life Test Sampling Plans—This section describes the procedures for use with life tests that are terminated at a specified time or upon the occurrence of a specified number of failures, if this number is reached before the specified time. Two procedures are given: (1) a procedure when testing without replacement and (2) another procedure when testing with replacement.

9.1.1 Use of Life Test Sampling Plans—To determine whether the lot meets the acceptability criterion with respect to average length of life, the applicable sampling plan shall be used in accordance with the provisions of Section 7 and those in this section.

9.1.2 Drawing of Samples—All samples shall be drawn in accordance with 6.6.

9.2 Selecting the Life Test Sampling Plan When Sampling Without Replacement:

9.2.1 Master Sampling Table—The master sampling tables for the life test sampling plans of this section are Tables A1.8-A1.12.

9.2.2 Obtaining the Sampling Plan—The life test sampling plan consists of a termination number, r , a sample size, n , and an associated termination time, T .

9.2.2.1 Termination Number—The termination number, r , shall be selected from among those given in Tables A1.8-A1.12 and specified before the initiation of the life test. The choice of this number shall be dependent on the degree of protection desired against acceptance of material with an unacceptable mean life. The larger the termination number, the larger the ratio θ_1/θ_0 and, as mentioned in 7.3.3, the greater the assurance against accepting material with an unacceptable mean life.

9.2.2.2 Sample Size—The choice of the sample size, as explained in 6.6.4, is dependent on the relative cost of placing a large number of units of product on test and the expected waiting time required for a decision. The sample size shall be selected with this factor in mind from one of the following multiples of the termination number: $2r$, $3r$, $4r$, $5r$, $6r$, $7r$, $8r$, $9r$, $10r$, and $20r$.

9.2.2.3 Termination Time—The termination time, T , corresponding to the applicable termination number, r , producer's risk, α , and sample size, n , is obtained from the master table by multiplying the tabled entry by the acceptable mean life, θ_0 .

9.3 Lot Acceptability Procedures When Testing Without Replacement:

9.3.1 Acceptability Criterion—The acceptability of a lot with respect to a life test from this section shall be judged by the time required for the r th failure to occur in a sample of size n . Compare the time of the occurrence of the r th failure with the termination time, T , mentioned in 9.2.2.3. If the r th failure occurs before time, T , the lot is considered to have failed to meet the acceptability criterion; if the r th failure still has not occurred by time, T , the lot is considered to have met the acceptability criterion.

9.4 Selecting the Life Test Plan When Testing With Replacement:

9.4.1 Master Sampling Table—The master sampling tables for the life test sampling plans with replacement are Tables A1.13-A1.17.

9.4.2 Obtaining the Sampling Plan—The truncated life test sampling plan consists of a termination number, r , a sample size, n , and an associated termination time, T .

9.4.2.1 Termination Number—The termination number, r , shall be selected from among those given in Tables A1.13-A1.17 and specified before the initiation of the life test. The choice of this number shall be dependent on the degree of protection desired against acceptance of material with unacceptable mean life. The larger the termination number, the larger the ratio, θ_1/θ_0 , and, as mentioned in 7.3.3, the greater the assurance against accepting material with an unacceptable mean life.

9.4.2.2 Sample Size—The choice of the sample size, as explained in 6.6.4, is dependent on the relative cost of placing a large number of units of product on test and the expected waiting time required for a decision. The sample size shall be selected with this factor in mind from one of the following multiples of the termination number: $2r$, $3r$, $4r$, $5r$, $6r$, $7r$, $8r$, $9r$, $10r$, and $20r$.

9.4.2.3 Termination Time—The termination time, T , corresponding to the applicable termination number, r , producer's risk, α , and sample size, n , is obtained from the master table by multiplying the tabled entry by the acceptable mean life, θ_0 .

9.5 Lot Acceptability Procedures when Testing with Replacement:

9.5.1 Acceptability Criterion—The acceptability of a lot with respect to a life test shall be judged by the time required for the r th failure to occur in a sample of size n . Compare the time of the occurrence of the r th failure with the termination time, T , mentioned in 9.4.2.3. If the r th failure occurs before time, T , the lot is considered to have failed to meet the acceptability criterion; if the r th failure still has not occurred by time, T , the lot is considered to have met the acceptability criterion.

9.5.1.1 Example 13: Testing Without Replacement—Find a life test sampling plan without replacement that will accept a lot having an acceptable mean life of 1000 h with probability 0.90. The experiment is to be stopped on the occurrence of the fifth failure, and ten units of product are to be placed on test.

9.5.1.2 Solution—In the notation of this practice, $\theta_0 = 1000$, $\alpha = 0.10$, $r = 5$, and $n = 10 = 2r$. From Table A1.10, $T = \theta_0(T/\theta_0) = 1000(0.314) = 314$. In word form, accept the lot if the fifth failure has not yet occurred by 314 h and reject the lot if the fifth failure occurs before 314 h have elapsed.

(1) The code designation of the life test sampling plan in 9.5.1.1 is obtained from Table A1.10 as C-5. From Fig. A1.1, the probability of accepting a lot with a mean life of, say, 500 h may be obtained by finding the ordinate of the OC curve labeled C-5 at the point where the abscissa $\theta/\theta_0 = 500/1000 = 0.5$. The probability of acceptance is seen to be equal to 0.47.

(2) In this example, if the termination number had been selected as 6 rather than 5, the probability of accepting a lot with mean life of 500 h is obtained from the OC curve labeled C-6. The probability is seen to equal 0.41. This illustrates the remark made in 9.2.2.1 that the larger the termination number, the higher the probability of rejecting lots with an unacceptable mean life.

9.5.1.3 Example 14: Testing With Replacement—In the problem of Example 13 (9.5.1.1), find the termination time if the failed units of product had been replaced.

9.5.1.4 Solution—From Table A1.15, $T = \theta_0(T/\theta_0) = 1000(0.243) = 243$ h. In word form, accept the lot if the fifth failure has not occurred by 243 h and reject the lot if the fifth failure occurs before 243 h have elapsed.

(1) The termination time when sampling with replacement in this example is 243 h as compared to 314 h when sampling without replacement. This illustrates the fact that the expected waiting time for a decision as to lot acceptability is lessened by testing with replacement.

9.6 Life Test Sampling Plans for Specified α , β , θ_1/θ_0 , and T/θ_0 —A life test sampling plan may be designed so that its OC curve meets the following prescribed conditions: (1) if $\theta = \theta_0$, then the probability of the lot meeting the acceptability criterion is $1 - \alpha$ and (2) if $\theta = \theta_1$, then the probability of the lot meeting the acceptability criterion is approximately equal to β . This section provides procedures for obtaining values of the termination number and the sample size when certain selected values of α , β , θ_1/θ_0 , and T/θ_0 are specified. This section may be considered an extension of 9.1-9.5, so that when values of α , β , θ_1/θ_0 , and T/θ_0 other than those provided here are needed, refer to 9.1-9.5 to determine whether one of the sampling plans given in that section is applicable. Moreover, if the desired value of T/θ_0 is not given in this section, note that T is usually an upper limit while θ_0 is a lower limit. Thus, if no sampling plan is given for the desired value of T/θ_0 , the sampling plan for the next lower value of T/θ_0 that is given may be used.

9.6.1 Life Test Plans When Testing Without Replacement—From Table A1.18, values of the termination number, r , and the sample size, n , may be obtained when testing without replacement for values of $\alpha = 0.01, 0.05, 0.10$, and 0.25 ; $\beta = 0.01, 0.05, 0.10$, and 0.25 ; $\theta_1/\theta_0 = 2/3, 1/2, 1/3, 1/5$, and $1/10$; and $T/\theta_0 = 1/3, 1/5, 1/10$, and $1/20$. The values of θ_1/θ_0 and T/θ_0 shall be computed and, for the appropriate values of α and β , values of r and n shall then be obtained from Table A1.18.

9.6.1.1 Example 15: Testing Without Replacement—Find a nonreplacement life test sampling plan that will not exceed 500 h and will accept a lot with an acceptable mean life of 10 000 h at least 90 % of the time but will reject a lot with an unacceptable mean life of 2000 h about 90 % of the time.

9.6.1.2 Solution—In this case, $T = 500$, $\theta_0 = 10\ 000$, $\theta_1 = 2000$, $\alpha = 0.10$, and $\beta = 0.10$. Hence, $\theta_1/\theta_0 = 1/5$ and $T/\theta_0 = 1/20$. Looking in Table A1.18 under $\alpha = 0.10$, $\beta = 0.10$, $\theta_1/\theta_0 = 1/5$, and $T/\theta_0 = 1/20$, the termination number, $r = 3$, and sample size, $n = 23$, are obtained. Thus, the desired nonreplacement plan is as follows: Start the life test with $n = 23$ units of product. Do not replace any units that fail. The lot is considered to have met the acceptability criterion if three failures have not occurred by 500 h and the life test is terminated at this time. The lot is considered to have failed to meet the acceptability criterion if the third failure occurs before 500 h and the test is terminated at the time of the third failure.

9.6.2 Life Test Plans When Testing With Replacement—From Table A1.19, values of the termination number, r , and the sample size, n , may be obtained when testing with replacement for values of $\alpha = 0.01, 0.05, 0.10$, and 0.25 ; $\beta = 0.01, 0.05,$

0.10 , and 0.25 ; $\theta_1/\theta_0 = 2/3, 1/2, 1/3, 1/5$, and $1/10$; and $T/\theta_0 = 1/3, 1/5, 1/10$, and $1/20$. The values θ_1/θ_0 and T/θ_0 shall be computed and, for the appropriate values of α and β , values of r and n shall then be obtained from Table A1.19.

9.6.2.1 Example 16: Testing With Replacement—Find a nonreplacement life test sampling plan that does not exceed 500 h and will accept a lot with a mean life of 10 000 h at least 90 % of the time but will reject a lot with a mean life of 2000 h about 90 % of the time.

9.6.2.2 Solution—In this problem, $T = 500$, $\theta_0 = 10\ 000$, $\theta_1 = 2000$, $\alpha = 0.10$, and $\beta = 0.10$. Hence, $\theta_1/\theta_0 = 1/5$ and $T/\theta_0 = 1/20$, the termination number $r = 3$, and the sample size, $n = 22$, are obtained. Thus, the desired test plan is as follows: Start the life test with $n = 22$ units of product. As soon as a unit of product fails, replace it with a new unit. The lot is considered to have met the acceptability criterion if 3 failures have not occurred by 500 h and the life test is terminated at this time. The lot is considered to have failed to meet the acceptability criterion if the third failure occurs before 500 h and the test is terminated at the time of the third failure.

9.7 Life Test Sampling Plans Based on Failure Rates—Fraction of Lot Failing before Specified Time—The sampling plans in this section may be used when either (1) the proportion of the lot failing before a specified time or (2) the failure rate during the time period is specified. Since the sampling plans are based on the proportion of the lot failing, when the failure rate for a period of time is specified, the failure rate shall be multiplied by the specified length of time. That is:

$$p = GT \quad (24)$$

where:

p = proportion of lot failing before specified time, T , and
 G = failure rate during period of time, T .

9.8 Life Test Sampling Plan—A lot may be considered satisfactory if the failure rate is less than or equal to p_0 and it may be considered unsatisfactory if the failure rate is greater than or equal to p_1 , where $p_1 > p_0$. From Table A1.20, values of the termination number r and the factor D are obtained when testing without replacement for values of $\alpha = 0.01, 0.05$, and 0.10 ; $\beta = 0.01, 0.05$, and 0.10 ; and $p_1/p_0 = 1.5, 2, 2.5, 3, 4, 5$, and 10 . In Table A1.20, the sample size, n , is given by $[D/p_0]$, which means the greatest integer less than or equal to D/p_0 , for example, $[3.8] = 3$ and $[4] = 4$.

9.8.1 Example 17: Testing Without Replacement—Find a nonreplacement life test sampling plan that will accept at least 90 % of the lots for which the failure rate for period of time, expressed as a percentage, is less than or equal to 1 % per 1000 h and will reject at least 95 % of the lots for which the failure rate is greater than or equal to 10 % per 1000 h.

9.8.2 Solution—In this problem, $G_0 = 0.01/1000 = 0.000\ 01$, $G_1 = 0.10/1000 = 0.000\ 10$, $\alpha = 0.0.10$, $\beta = 0.05$, and $T = 1000$ h. Thus, $p_0 = 1000$, $G_0 = 0.01$, $p_1 = 1000$, $G_1 = 0.10$, and $p_1/p_0 = 10$. Looking at Table A1.20, it is seen that $r = 2$ and $n = [0.532/0.01] = 53$. Thus, the desired plan is as follows: Place 53 units of product on test. If 2 failures occur before time, T , reject the lot and terminate the test at the time of occurrence of the second failure. If one or fewer failures have occurred at time, T , accept the lot and terminate the test.

10. Sequential Life Test Sampling Plans

10.1 Sequential Life Test Sampling Plans—This section describes the procedures for use in determining lot acceptability with sequential life tests. Two procedures are given: (1) a procedure when testing without replacement and (2) another procedure when testing with replacement.

10.1.1 Use of Sequential Life Test Plans—To determine whether the lot meets the acceptability criterion with respect to average length of life, the applicable sampling plan shall be used in accordance with the provisions of Section 7 and those in this section.

10.1.2 Drawing of Samples—All samples shall be drawn in accordance with 6.6.

10.1.3 Sample Plan Code Designation—The sample plan code designation shall be selected from Table A1.1.

10.2 Selecting Sequential Life Test Plans for Determining Lot Acceptability:

10.2.1 Master Sampling Table—The master sampling tables for sequential life test plans for determining acceptability of a lot are Tables A1.21-A1.25.

10.2.2 Obtaining the Sampling Plan—The sequential life test sampling plan consists of a sample size, n , the acceptance line intercept, h_0 , the rejection line intercept, h_1 , and the common slope, s , of the two lines. The sampling plan is obtained from the master table.

10.2.2.1 Sample Size—The minimum number of units of product that shall be placed on test, r_0 , when testing without replacement, is shown in the master table. When testing with replacement, the sample may be of any size. Increasing the sample size, in either sampling with or without replacement, will decrease the time required to reach a decision as to lot acceptability.

10.2.2.2 Acceptance Line Intercept—The acceptance line intercept, h_0 , is obtained from the master table by multiplying the entry corresponding to the sample plan code designation by the acceptable mean life, θ_0 .

10.2.2.3 Rejection Line Intercept—The rejection line intercept, h_1 , is obtained from the master table by multiplying the entry corresponding to the sample plan code designation by θ_0 .

10.2.2.4 Slope of Decision Lines—The common slope, s , of the acceptance and rejection lines is obtained from the master table by multiplying the entry corresponding to the sample plan code designation by θ_0 .

10.2.3 Acceptance Time—The acceptance time

$$h_0 + ks \quad (25)$$

where:

h_0 = acceptance line intercept obtained in 10.2.2.2,
 s = slope of the decision lines as obtained in 10.2.2.4, and
 k = number of failed units of product observed in the length of time that the life test has been in progress.
 shall be computed for $k = 0, 1, 2, \dots$

10.2.4 Rejection Time—The rejection time

$$h_1 + ks \quad (26)$$

where:

h_1 = rejection line intercept obtained in 10.2.2.3,
 s = slope of the decision lines as obtained in 10.2.2.4, and

k = number of failed units of product observed in the length of time that the life test has been in progress.

shall be computed for $k = 0, 1, 2, \dots$. Negative values of the rejection time mean that more failures shall occur before the rejection of the lot is allowed and hence may be disregarded.

10.3 Lot Acceptability Procedures When Testing Without Replacement:

10.3.1 Total Life—The acceptability of a lot with respect to a sequential life test shall be judged by the quantity, $V(t)$.

10.3.2 Computation—The following quantity shall be computed from the test results:

$$V(t) = \sum_{i=1}^k x_{i,n} + (n - k)t \quad (27)$$

where:

$x_{i,n}$ = time of the i th failure in a sample of size n ,
 t = length of time that the life test has been in progress,
 k = number of failed units of product observed in time t , and
 $V(t)$ = total length of time survived by all units of product on test, failed and unfailed, up to time, t .

10.3.3 Acceptability Criterion—Compare the quantity $V(t)$ with the acceptance time mentioned in 10.2.3 and with the rejection time mentioned in 10.2.4. If $V(t)$ is equal to or greater than $h_0 + ks$, the lot meets the acceptability criterion; if $V(t)$ is less than or equal to $h_1 + ks$, the lot does not meet the acceptability criterion; and if $h_1 + ks < V(t) < h_0 + ks$, the evidence is insufficient to reach a decision as to acceptability so the life test shall continue and the procedures in 10.3 repeated at a later time, t .

10.4 Lot Acceptability Procedures When Testing With Replacement:

10.4.1 Total Life—The acceptability of a lot with respect to a sequential life test shall be judged by the quantity, $V(t)$.

10.4.2 Computation—The following quantity shall be computed from the test results:

$$V(t) = nt \quad (28)$$

where:

n = number of units of product placed on test originally,
 t = length of time that the life test has been in progress, and
 $V(t)$ = total length of time survived by all units of product, failed and unfailed, original units and replacement units, up to time, t .

10.4.3 Acceptability Criterion—Compare the quantity, $V(t)$, with the acceptance time mentioned in 10.2.3 and with the rejection time mentioned in 10.2.4. If $V(t)$ is equal to or greater than $h_0 + ks$, the lot meets the acceptability criterion; if $V(t)$ is less than or equal to $h_1 + ks$, the lot does not meet the acceptability criterion; and if $h_1 + ks < h_0 + ks$, the evidence is insufficient to reach a decision as to acceptability so the life test shall continue and the procedures in 10.4 repeated at a later time, t .

10.5 Choice of Times for Determining Acceptability—The procedures of 10.3 and 10.4 allow the acceptance of the lot if no failures are observed before time, h_0/n , has elapsed; rejection of the lot is allowed at any time, $t > 0$, but the number of failures shall exceed $-h_1/s$. If decisions as to lot acceptability

can be made continuously in time, the greatest savings in expected waiting time and the number of failures required for decision are realized over the procedures of Sections 8 and 9. However, if acceptance of the lot has not been allowed at time, h_0/n , computation of $V(t)$ mentioned in 10.3.2 or 10.4.2 may be made periodically. The computation of $V(t)$ shall follow each failure but may be made more often to reduce the waiting time required for decision.

10.6 Truncation of Sequential Life Tests—The sequential life test, when testing without replacement, will terminate, at the latest, when all units of product placed on test have failed; the sequential life test, when testing with replacement, should not be allowed to run indefinitely but may be terminated by the procedures of this paragraph. In either case, the sequential life test may be terminated and the lot considered to have met the acceptability criterion if the number of failures is less than r_0 , where the value of r_0 is obtained from Tables A1.21-A1.25 and if:

$$V(t) \geq \min(h_0 + ks, sr_0) \quad (29)$$

where:

s and $V(t)$ are explained in 10.2.2.4 and 10.3.2 or 10.4.2, and $\min(h_0 + ks, sr_0)$ = lesser of either $h_0 + ks$ or sr_0 .

10.6.1 The sequential life test shall be terminated and the lot considered to have failed to meet the acceptability criterion if $V(t) < h_0 + ks$ or if the number of failures equals r_0 and $V(t) < sr_0$.

10.7 Graphical Acceptance Procedures:

10.7.1 Charts Made before Start of Life Test—The acceptability procedures of 10.2-10.6 may be drawn on a chart with the vertical axis representing $V(t)$ and the horizontal axis representing k (see Example 20 in 10.9.7 and Fig. A1.2). The acceptance line shall be drawn with vertical axis intercept equal to h_0 and with slope, s . The rejection line shall be drawn with vertical axis intercept, h_1 and with slope, s . If the sequential test is to be truncated, a horizontal line shall be drawn at $V(t) = sr_0$ from the acceptance line to the point (r_0, sr_0) . From this point, a vertical line is drawn to the rejection line (see Example 21 in 10.9.9 and Fig. A1.3).

10.7.2 Plotting of Data—The life test data, $V(t)$, as obtained by the procedures of 10.3.2 or 10.4.2 shall be plotted on the chart prepared in accordance with 10.7.1 by moving vertically as long as the next failure is being awaited and moving horizontally by one unit (in k) at the occurrence of each failure. The life test continues until the plotted data touches one of the lines already drawn on the chart. If the plotted data touches the acceptance line or the horizontal line $V(t) = sr_0$ at a point to the left of (r_0, sr_0) , the lot meets the acceptability criterion. If the plotted data touches the rejection line or the vertical line below the point (r_0, sr_0) , the lot does not meet the acceptability criterion.

10.8 Expected Number of Failures Required for Decision—The expected number of failures required for a decision as to lot acceptability is dependent on the mean life of the lot. The master table gives the expected numbers of failures required when the mean life is equal to 0, θ_1 , s (the mean life whose numerical value is equal to the slope of 10.2.2.4), and θ_0 and are denoted by $E_0(r)$, $E_{\theta_1}(r)$, $E_s(r)$, and $E_{\theta_0}(r)$, respectively. These values apply whether the testing is with or without

replacement and assume that the decisions are made continuously in time. If $V(t)$ is computed periodically, the expected values may be exceeded.

10.9 Expected Waiting Time Required for Decision—The expected waiting time required for a decision as to lot acceptability is dependent on the mean life of the lot and the number of units of product placed on test. When testing without replacement, the expected waiting times, when $\theta = 0$, θ_1 , s , and θ_0 , are given approximately by:

$$E_0(t) = 0 \quad (30)$$

$$E_{\theta_1}(t) \cong \theta_1 \log_e \{n/[n - E_{\theta_1}(r)]\}$$

$$E_s(t) \cong s \log_e \{n/[n - E_s(r)]\}$$

$$E_{\theta_0}(t) \cong \theta_0 \log_e \{n/[n + E_{\theta_0}(r)]\}$$

10.9.1 When testing with replacement, the expected waiting times are given by:

$$E_0(t) = 0 \quad (31)$$

$$E_{\theta_1}(t) = \theta_1 E_{\theta_1}(r)/n$$

$$E_s(t) = s E_s(r)/n$$

$$E_{\theta_0}(t) = \theta_0 E_{\theta_0}(r)/n$$

10.9.2 These values are based on the assumption that the decisions are made continuously in time so that if $V(t)$ is computed only periodically, the expected values may be exceeded.

10.9.3 Example 18: Selection of Sequential Life Test Plan—Find a sequential replacement procedure that will accept a lot with acceptable mean life $\theta_0 = 1500$ h 95 % of the time and will reject a lot with unacceptable mean life $\theta_1 = 300$ h 90 % of the time. In this case, $\theta_0 = 1500$, $\theta_1 = 300$, $\alpha = 0.05$, and $\beta = 0.10$.

10.9.4 Solution—Since $\theta_1/\theta_0 = 300/1500 = 0.200$, Table A1.1 gives sequential life test Plan B-4 as the proper plan to be used. From Tables A1.21-A1.25, the following quantities are obtained: $h_0 = \theta_0(h_0/\theta_0) = 1500(0.5805) = 870.75$ h, $h_1 = \theta_0(h_1/\theta_0) = 1500(0.7453) = 1117.95$ h, $s = \theta_0(s/\theta_0) = 1500(0.4086) = 612.9$ h/failure, and minimum $n = r_0 = 12$. Substituting in the formula of 10.4.2 and 10.4.3, the life test is continued as long as the inequality $-1117.95 + 612.9 k > nt > 870.75 + 612.9 k$ holds and is stopped as soon as the inequality does not hold. If 20 units of product are placed on test, the inequality may be written $-55.90 + 30.64 k > t > 43.54 + 30.64 k$.

10.9.4.1 If, at the time of stopping, t is less than the left-hand member of the inequality, the lot is considered to have failed to meet the acceptability criterion; if, at the time of stopping, t is greater than the right-hand member of the inequality, the lot is considered to have met the acceptability criterion.

10.9.5 Example 19: Expected Number of Failures and Waiting Time—Determine the expected number of failures and the expected waiting time required for a decision in the sequential life test plan of Example 18 in 10.9.3 if $n = 20$ and the mean life of the lot is 0, θ_1 , s , and θ_0 h.

10.9.6 Solution—From Tables A1.21-A1.25, for sequential Plan B-4:

$$E_0(r) = 1.8 \text{ units of product} \quad (32)$$

$$E_{\theta_1}(r) = 3.0 \text{ units of product}$$

$$E_s(r) = 2.6 \text{ units of product}$$

$$E_{\theta_0}(r) = 0.9 \text{ units of product}$$

10.9.6.1 From the formulas of 10.9:

$$E_0(r) = 0 \text{ hours} \quad (33)$$

$$E_{\theta_1}(r) = 310(3.0)/20 = 46.5 \text{ hours}$$

$$E_s(r) = (612.9)(2.6)/20 = 79.7 \text{ hours}$$

$$E_{\theta_0}(r) = 1500(0.9)/20 = 67.5 \text{ hours}$$

10.9.7 *Example 20: Sequential Life Test Plan*—In the problem of Example 18 in 10.9.3, suppose that a sample of size 20 is placed on test. New units of product drawn from the same lot replace units of product that fail immediately. The life test is started at time $t = 0$ and the first five failures occur at $x_{1,20} = 25$ h, $x_{2,20} = 55$ h, $x_{3,20} = 70$ h, $x_{4,20} = 100$ h, and $x_{5,20} = 160$ h, all times being measured from $t = 0$.

10.9.7.1 Verify that no decision has been reached by time, $x_{5,20}$.

10.9.7.2 Verify that if the sixth failure has not occurred at 196.74 h, measured from $t = 0$, the life test may be terminated at that time with acceptance of the lot.

10.9.8 *Solution*—The acceptance procedure, as described in 10.7, is drawn in Fig. A1.2. The plotted data is still within the two decision lines at time $x_{5,20} = 160$ or $V(t) = 20(160) = 3200$ but crosses the acceptance line when $k = 5$ at time $t = 43.54 + 30.64(5) = 196.74$ since $t = V(t)/n$. Since the sixth failure has not yet occurred, the life test may be terminated at $t = 196.74$ h with the acceptance of the lot.

10.9.8.1 If the sixth failure had occurred at $t = 225$ h, the time saved by making decisions continuously in time is $225 - 196.74 = 28.26$ h. Thus, if $V(t)$ is computed only after occurrence of a failure, the life test would have been prolonged 28.26 h needlessly.

10.9.9 *Example 21: Truncated Sequential Life Test Plan*—In the problem of Example 18 in 10.9.3, suppose that the sequential life test plan is truncated and a sample of size 20 is placed on test at time $t = 0$. The first twelve failures occur at

25, 55, 70, 100, 160, 190, 200, 225, 235, 290, 320, and 335 h. Verify that the lot does not meet the acceptability criterion.

10.9.10 *Solution*—The acceptance procedure, as described in 10.7, is drawn in Fig. A1.3. The plotted data crosses the vertical line below the point (r_0, sr_0) or (12 7354.8), so the lot does not meet the acceptability criterion.

10.9.10.1 While the acceptance of the lot in Example 20 is made between failure times $x_{5,20}$ and $x_{6,20}$, rejection of the lot in Example 21 in 10.9.9 is made at the failure time $x_{12,20}$. This illustrates the point that acceptance of a lot can always be made between failure times, whereas rejection of a lot can only be made at a failure time.

10.10 *Comparison of Expected Number of Failures and Expected Waiting Times Required for a Decision between Life Tests Terminated at a Preassigned Time:*

10.10.1 In Fig. A1.4, a comparison is shown in the expected number of failures required for a decision between a life test terminated at preassigned time when sampling with replacement plan of Section 9 and that for a sequential plan of Section 10. Both plans have OC curves passing through the points $(\theta_0 = 1500, 1 - \alpha = 0.95)$ and $(\theta_1 = 300, \beta = 0.10)$.

10.10.2 In Fig. A1.5, a comparison is shown in the expected waiting times required for a decision between a life test terminated at preassigned time when sampling with replacement plan and a sequential replacement plan. Both plans have sample size $n = 20$ and OC curves passing through the points $(\theta_0 = 1500, 1 - \alpha = 0.95)$ and $(\theta_1 = 300, \beta = 0.10)$.

10.10.3 The above comparisons are typical of the savings in time and number of failures required for a decision.

11. Keywords

11.1 acceptability constant; acceptance sampling; acceptance time; consumer's risk; exponential distribution; failure rate; hazard rate; life test; mean life; mean time to failure; OC; operating characteristic; producer's risk; rejection time; reliability; sample size; sampling plan; sequential life test; termination number; testing with replacement; testing without replacement; total life

ANNEX

(Mandatory Information)

A1. TABLES AND FIGURES

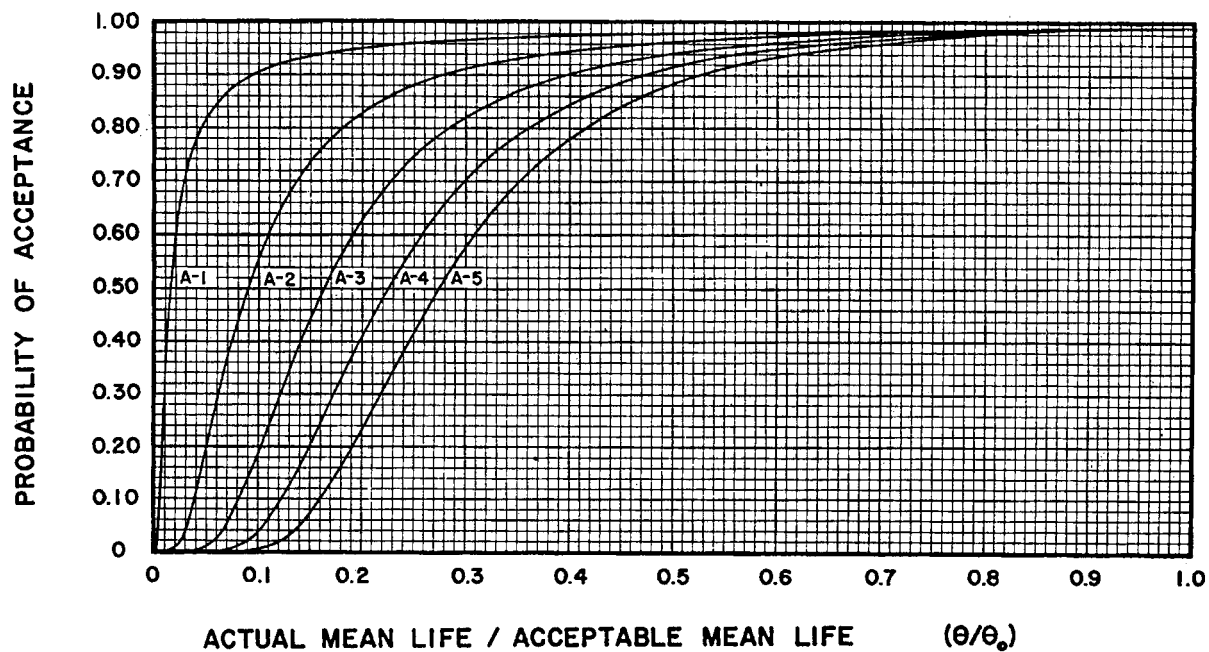
Table A1.1	Life Test Sampling Plan Code Designation
Fig. A1.1	Operating Characteristic Curves for Life Tests Terminated Upon Occurrence of Preassigned Number of Failures
Table A1.2	Master Table for Life Tests Terminated Upon Occurrence of Preassigned Number of Failures
Tables A1.3 and A1.4	Life Tests Terminated Upon Occurrence of Preassigned Number of Failures Testing Without Replacement
Table A1.5	Expected Relative Saving Time by Increasing Sample Size
Table A1.6	Expected Relative Saving in Time by Testing With Replacement
Table A1.7	Life Test Sampling Plans for Specified α , β , and θ_1/θ_0
Tables A1.8-A1.12	Master Tables for Life Tests Terminated at Preassigned Time—Testing Without Replacement
Tables A1.13-A1.17	Master Tables for Life Tests Terminated at Preassigned Time—Testing With Replacement
Table A1.18	Life Tests Terminated at Preassigned Time—Testing Without Replacement, Life Test Sampling Plans for Specified α , β , θ_1/θ_0 , and T/θ_0
Table A1.19	Life Tests Terminated at Preassigned Time—Testing With Replacement, Life Test Sampling Plans for Specified α , β , θ_1/θ_0 , and T/θ_0
Table A1.20	Life Tests Terminated at Preassigned Time—Testing Without Replacement, Life Test Sampling Plans for Specified α , β , and p_1/p_0
Fig. A1.2	Example of Sequential Life Test
Fig. A1.3	Example of Truncated Sequential Life Test
Tables A1.21-A1.25	Master Tables for Sequential Life Tests
Fig. A1.4	Comparison of Expected Number of Failures Required for Decision for Sequential and Life Test Terminated at Preassigned Time, Sampling With Replacement Plans
Fig. A1.5	Comparison of Expected Waiting Time Required for Decision for Sequential and Life Test Terminated at Preassigned Time, Sampling With Replacement Plans

TABLE A1.1 Live Test Sampling Plan Code Designation

NOTE 1—Producer's risk α is the probability of rejecting lots with mean life θ_0 .
NOTE 2—Consumer's risk β is the probability of accepting lots with mean life θ_1 .

Index of Life Test Sampling Plans of Section 8, Section 9, and Section 10 OC curves are given for these sampling plans in Fig. A1.1									
$\alpha = 0.01$ $\beta = 0.10$		$\alpha = 0.05$ $\beta = 0.10$		$\alpha = 0.10$ $\beta = 0.10$		$\alpha = 0.25$ $\beta = 0.10$		$\alpha = 0.50$ $\beta = 0.10$	
Code	θ_1/θ_0	Code	θ_1/θ_0	Code	θ_1/θ_0	Code	θ_1/θ_0	Code	θ_1/θ_0
A-1	0.004	B-1	0.022	C-1	0.046	D-1	0.125	E-1	0.301
A-2	0.038	B-2	0.091	C-2	0.137	D-2	0.247	E-2	0.432
A-3	0.082	B-3	0.154	C-3	0.207	D-3	0.325	E-3	0.502
A-4	0.123	B-4	0.205	C-4	0.261	D-4	0.379	E-4	0.550
A-5	0.160	B-5	0.246	C-5	0.304	D-5	0.421	E-5	0.584
A-6	0.193	B-6	0.282	C-6	0.340	D-6	0.455	E-6	0.611
A-7	0.221	B-7	0.312	C-7	0.370	D-7	0.483	E-7	0.633
A-8	0.247	B-8	0.338	C-8	0.396	D-8	0.506	E-8	0.652
A-9	0.270	B-9	0.361	C-9	0.418	D-9	0.526	E-9	0.667
A-10	0.291	B-10	0.382	C-10	0.438	D-10	0.544	E-10	0.681
A-11	0.371	B-11	0.459	C-11	0.512	D-11	0.608	E-11	0.729
A-12	0.428	B-12	0.512	C-12	0.561	D-12	0.650	E-12	0.759
A-13	0.470	B-13	0.550	C-13	0.597	D-13	0.680	E-13	0.781
A-14	0.504	B-14	0.581	C-14	0.624	D-14	0.703	E-14	0.798
A-15	0.554	B-15	0.625	C-15	0.666	D-15	0.737	E-15	0.821
A-16	0.591	B-16	0.658	C-16	0.695	D-16	0.761	E-16	0.838
A-17	0.653	B-17	0.711	C-17	0.743	D-17	0.800	E-17	0.865
A-18	0.692	B-18	0.745	C-18	0.774	D-18	0.824	E-18	0.882

(Curves for sequential plans and tests terminated at pre-assigned time are essentially equivalent)

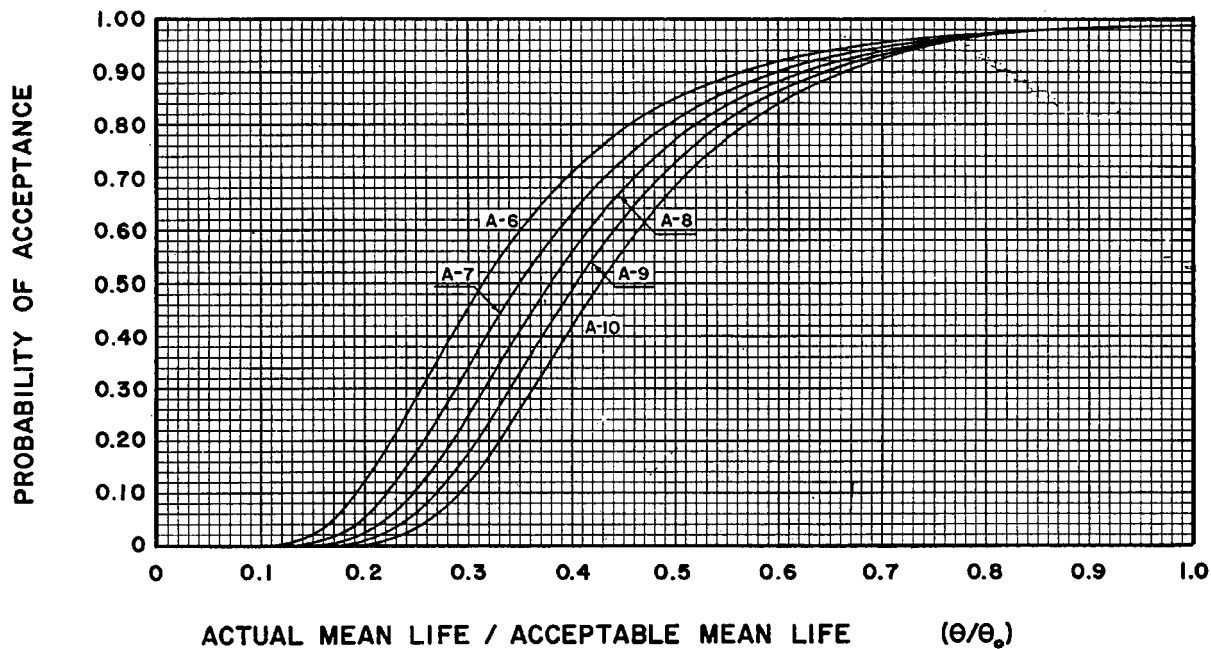


These curves are valid only when sampling from an exponential distribution.

Note: Notations on curves are sample plan code designation

FIG. A1.1 Operating Characteristic Curves for Life Tests Terminated Upon Occurrence of Preassigned Number of Failures

(Curves for sequential plans and tests terminated at pre-assigned time are essentially equivalent)

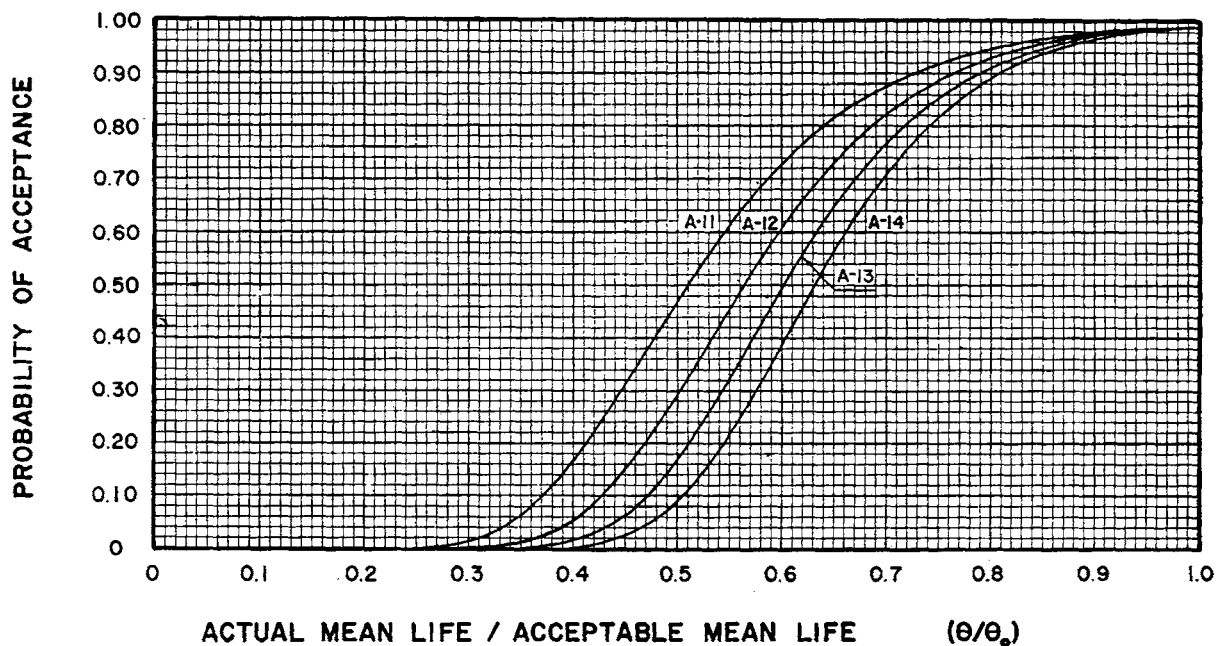


These curves are valid only when sampling from an exponential distribution.

Note: Notations on curves are sample plan code designation

FIG. A1.1 Operating Characteristic Curves for Life Tests Terminated Upon Occurrence of Preassigned Number of Failures (continued)

(Curves for sequential plans and tests terminated at pre-assigned time are essentially equivalent)

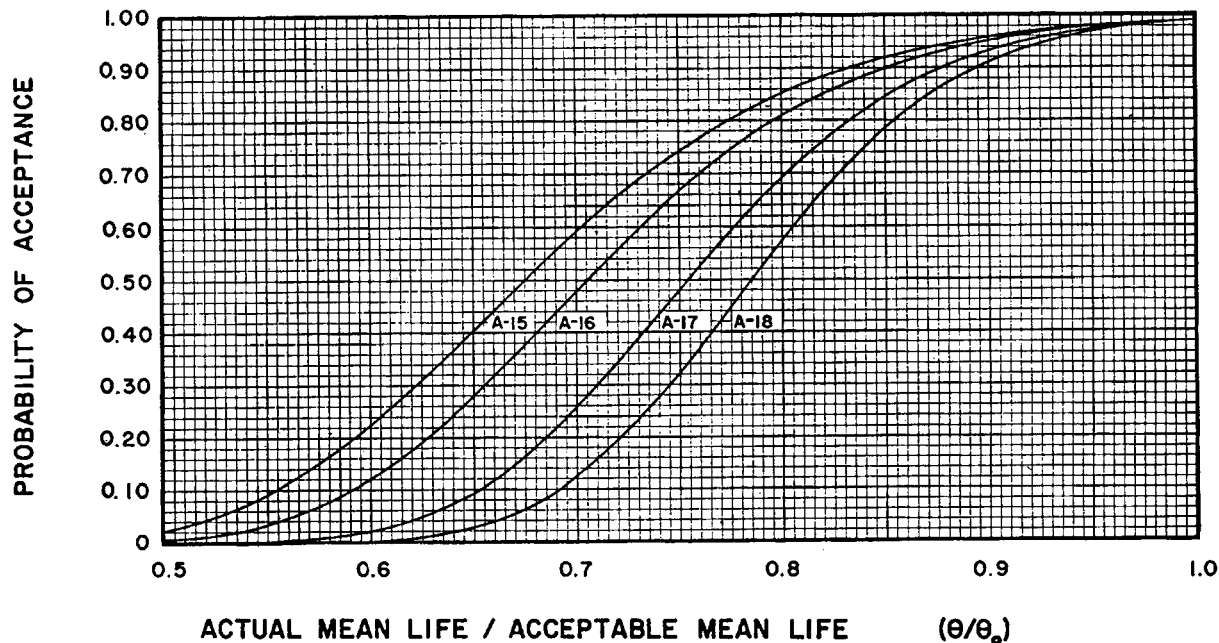


These curves are valid only when sampling from an exponential distribution.

Note: Notations on curves are sample plan code designation

FIG. A1.1 Operating Characteristic Curves for Life Tests Terminated Upon Occurrence of Preassigned Number of Failures (continued)

(Curves for sequential plans and tests terminated at pre-assigned time are essentially equivalent)



These curves are valid only when sampling from an exponential distribution.

Note: Notations on curves are sample plan code designation

FIG. A1.1 Operating Characteristic Curves for Life Tests Terminated Upon Occurrence of Preassigned Number of Failures (continued)

(Curves for sequential plans and tests terminated at pre-assigned time are essentially equivalent)

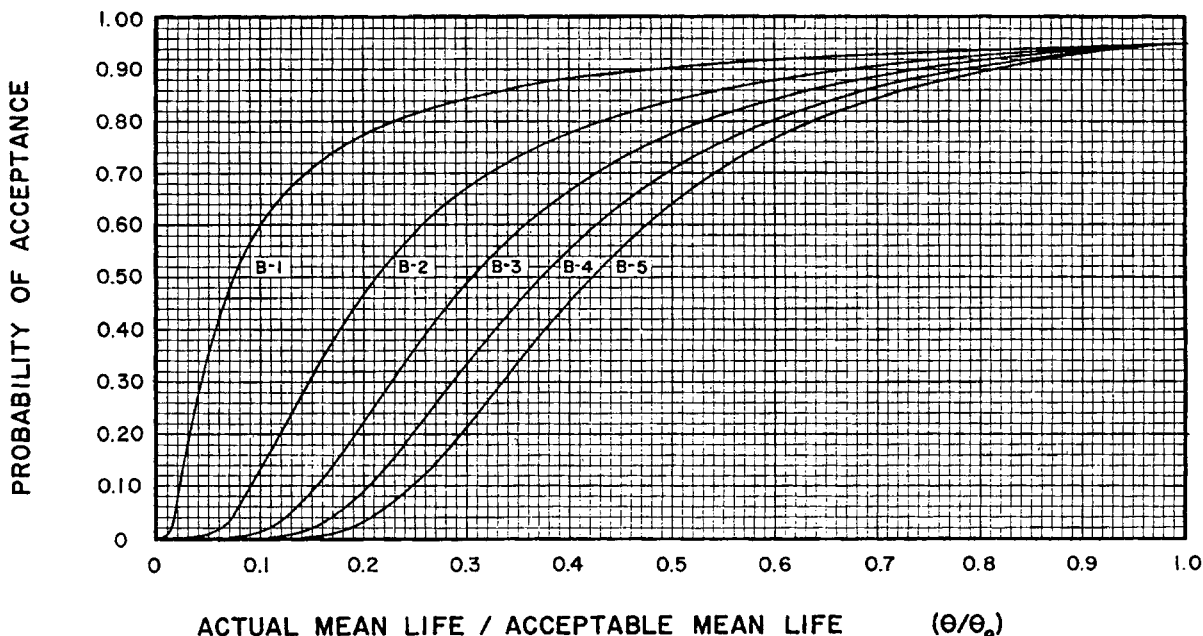


FIG. A1.1 Operating Characteristic Curves for Life Tests Terminated Upon Occurrence of Preassigned Number of Failures (continued)

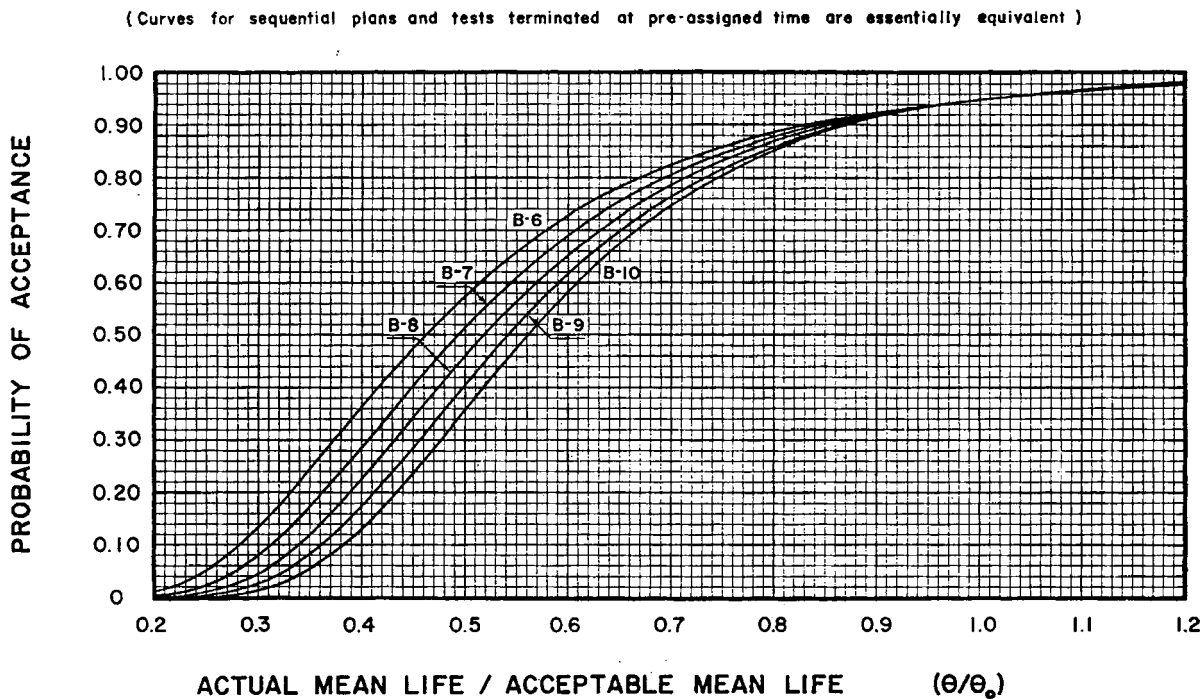
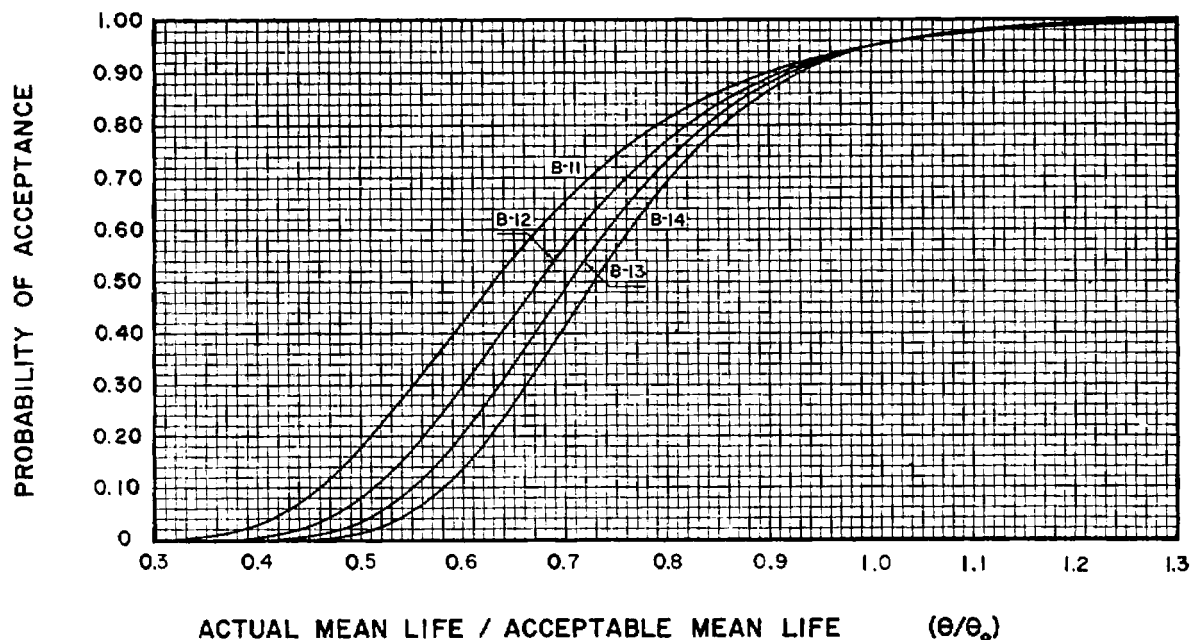


FIG. A1.1 Operating Characteristic Curves for Life Tests Terminated Upon Occurrence of Preassigned Number of Failures (continued)

(Curves for sequential plans and tests terminated at pre-assigned time are essentially equivalent)

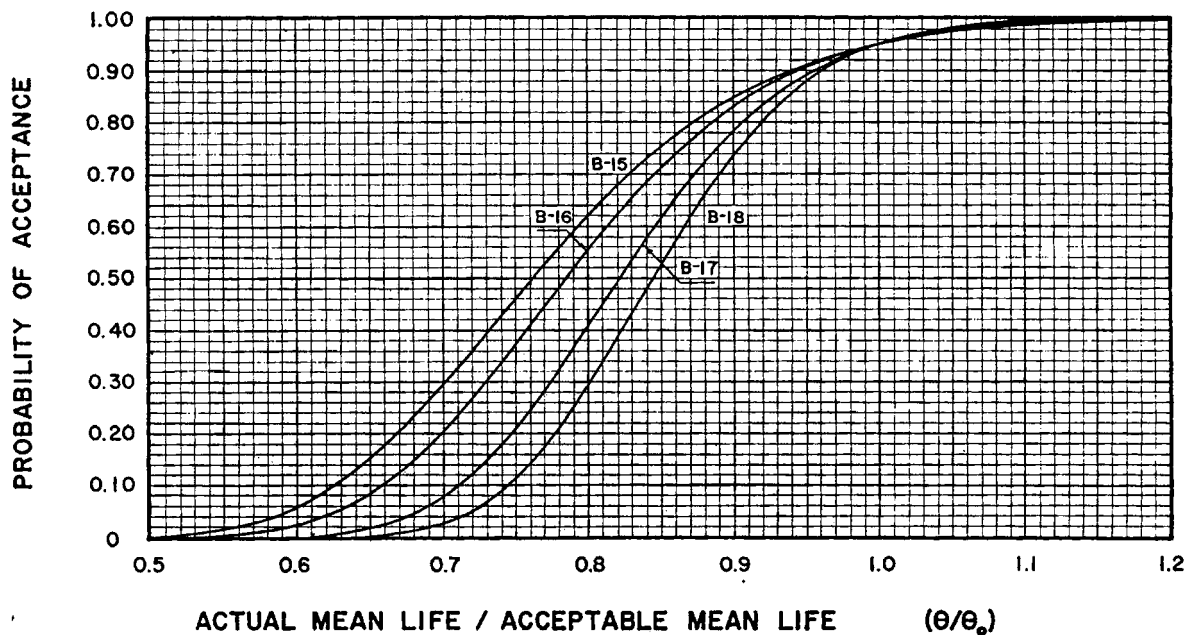


These curves are valid only when sampling from an exponential distribution.

Note: Notations on curves are sample plan code designation

FIG. A1.1 Operating Characteristic Curves for Life Tests Terminated Upon Occurrence of Preassigned Number of Failures (continued)

(Curves for sequential plans and tests terminated at pre-assigned time are essentially equivalent)



These curves are valid only when sampling from an exponential distribution.

Note: Notations on curves are sample plan code designation

FIG. A1.1 Operating Characteristic Curves for Life Tests Terminated Upon Occurrence of Preassigned Number of Failures (continued)

(Curves for sequential plans and tests terminated at pre-assigned time are essentially equivalent)

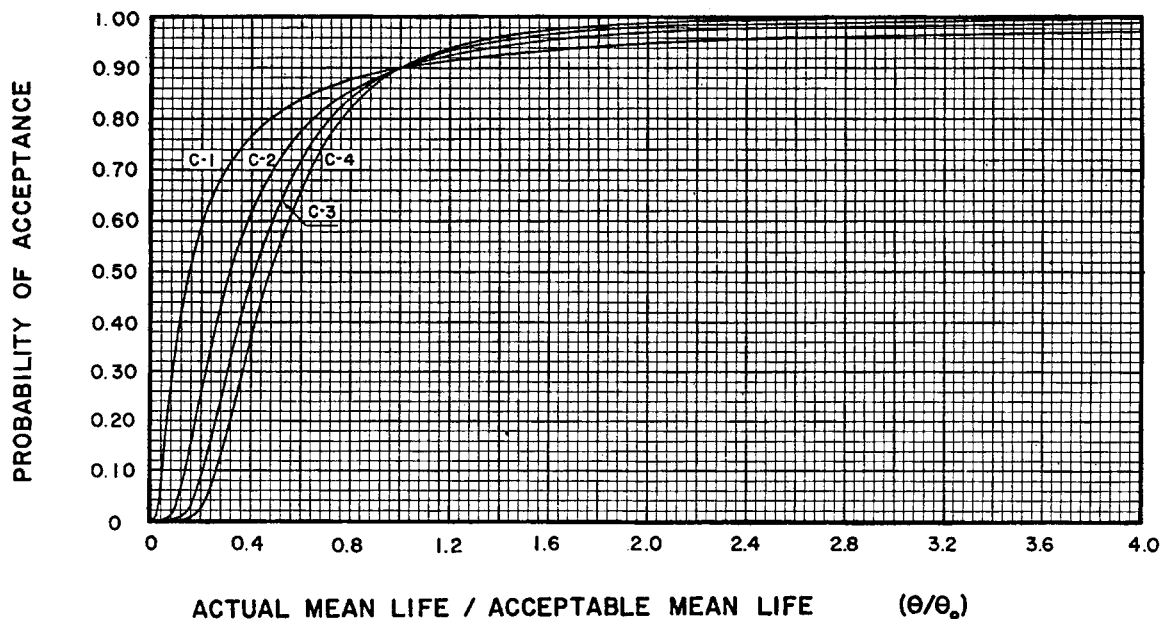


FIG. A1.1 Operating Characteristic Curves for Life Tests Terminated Upon Occurrence of Preassigned Number of Failures (continued)

(Curves for sequential plans and tests terminated at pre-assigned time are essentially equivalent)

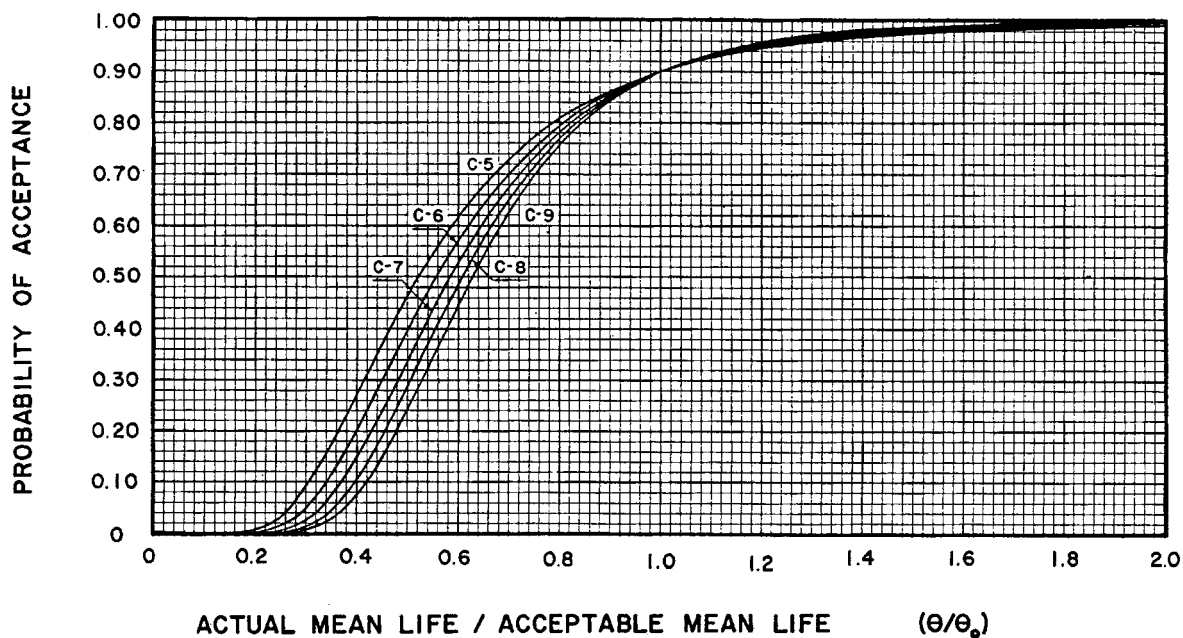
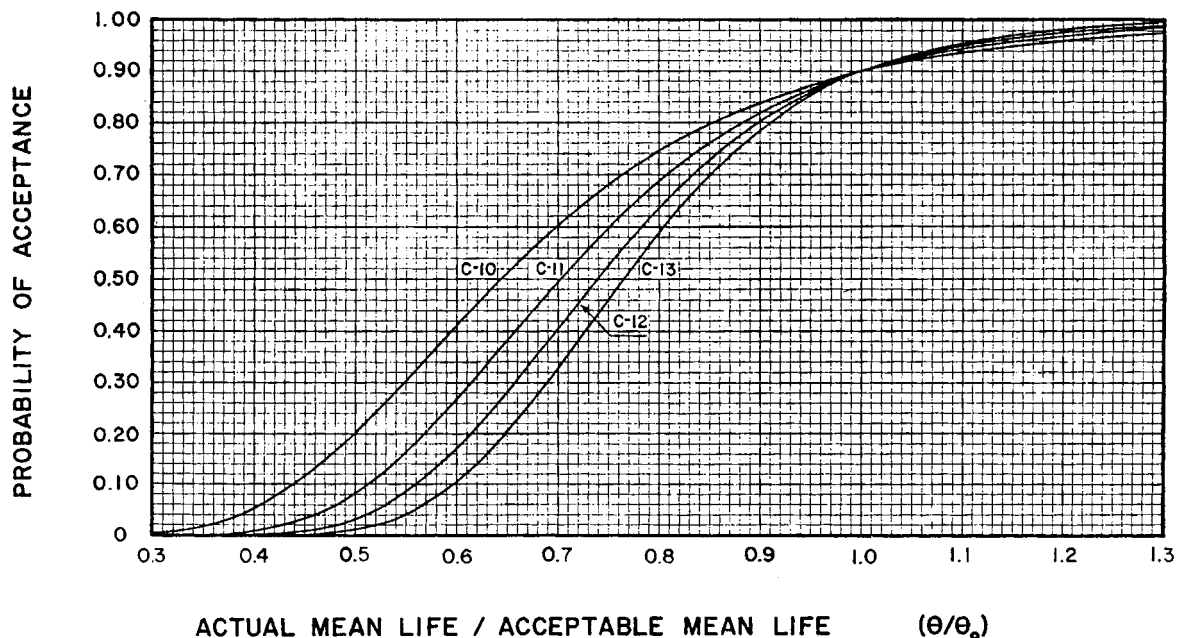


FIG. A1.1 Operating Characteristic Curves for Life Tests Terminated Upon Occurrence of Preassigned Number of Failures (continued)

(Curves for sequential plans and tests terminated at pre-assigned time are essentially equivalent)

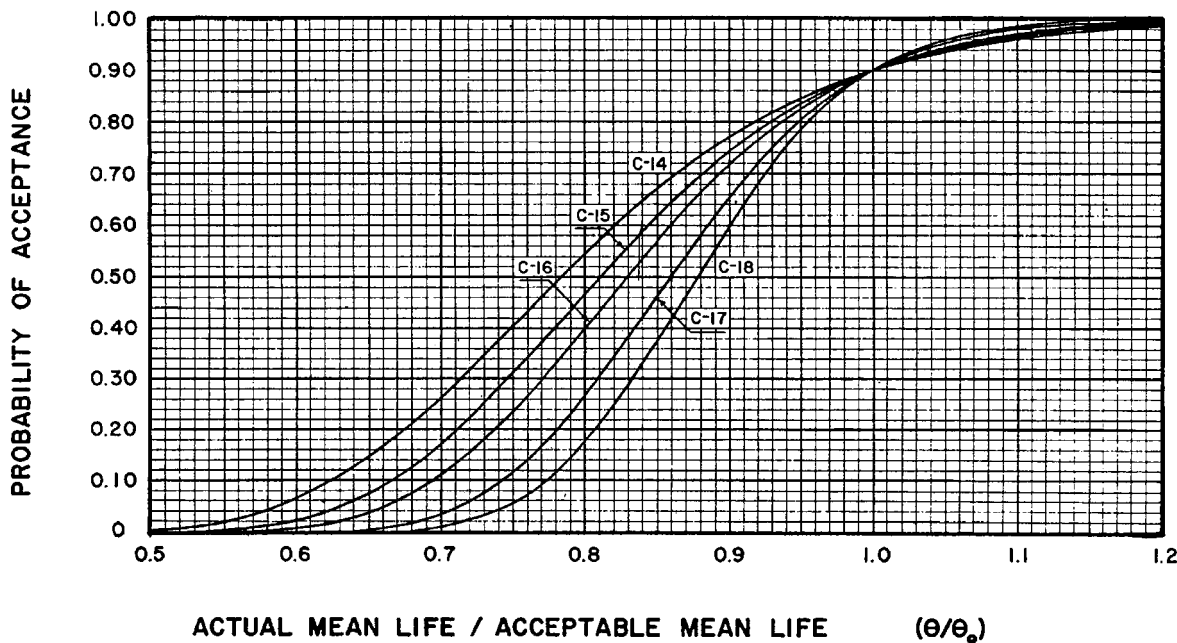


These curves are valid only when sampling from an exponential distribution.

Note: Notations on curves are sample plan code designation

FIG. A1.1 Operating Characteristic Curves for Life Tests Terminated Upon Occurrence of Preassigned Number of Failures (continued)

(Curves for sequential plans and tests terminated at pre-assigned time are essentially equivalent)

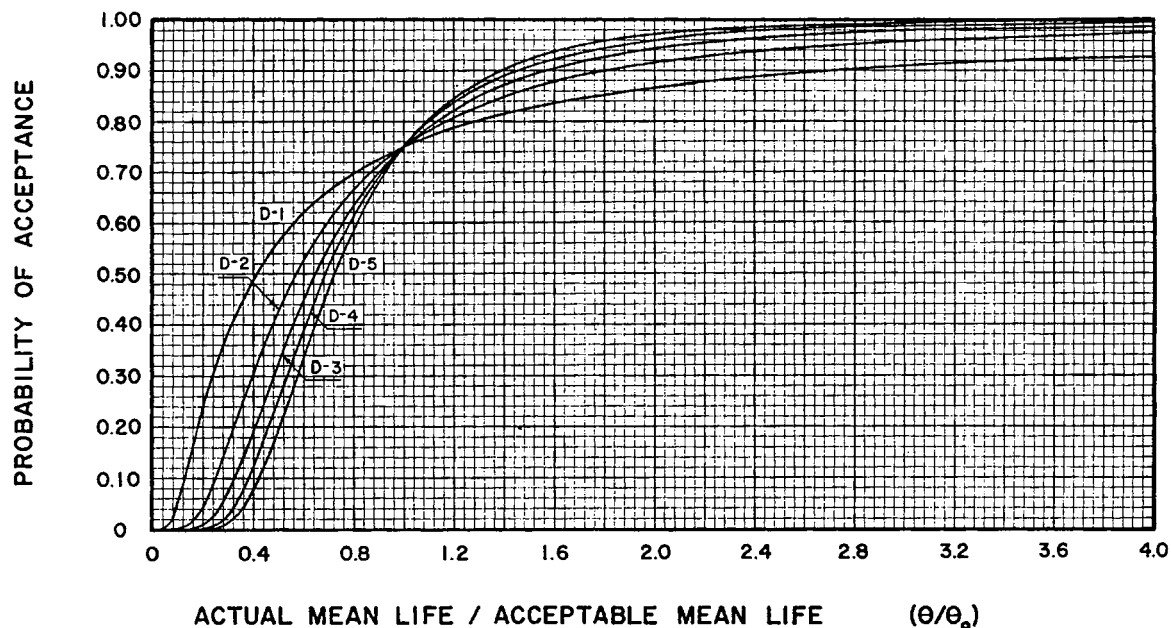


These curves are valid only when sampling from an exponential distribution.

Note: Notations on curves are sample plan code designation

FIG. A1.1 Operating Characteristic Curves for Life Tests Terminated Upon Occurrence of Preassigned Number of Failures (continued)

(Curves for sequential plans and tests terminated at pre-assigned time are essentially equivalent)

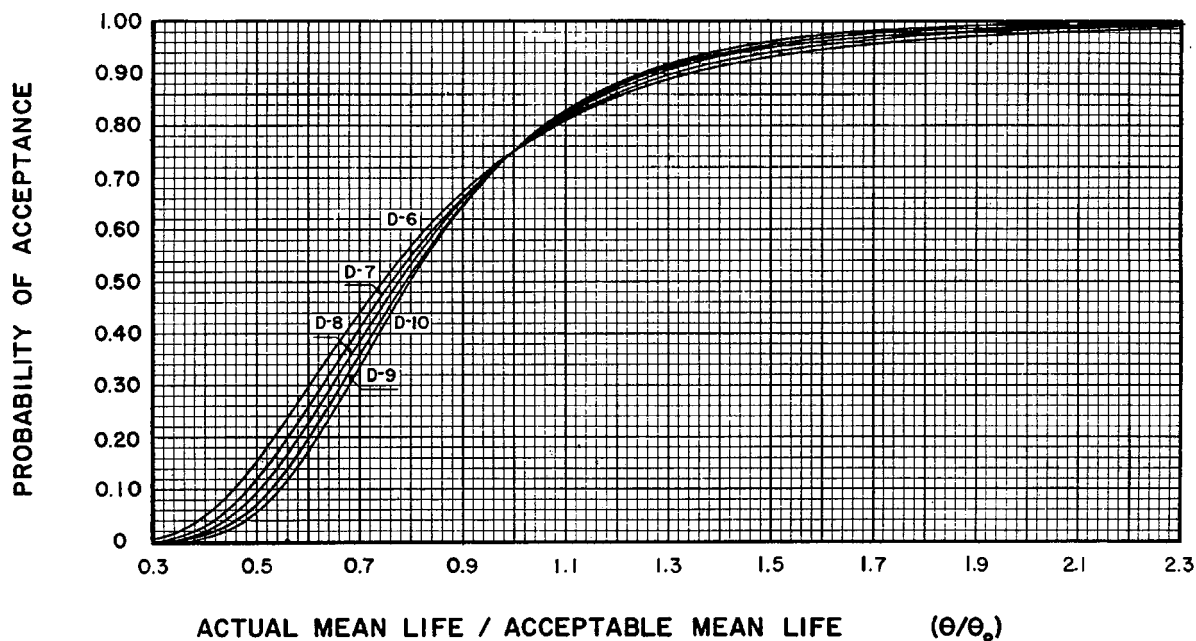


These curves are valid only when sampling from an exponential distribution.

Note: Notations on curves are sample plan code designation

FIG. A1.1 Operating Characteristic Curves for Life Tests Terminated Upon Occurrence of Preassigned Number of Failures (continued)

(Curves for sequential plans and tests terminated at pre-assigned time are essentially equivalent)

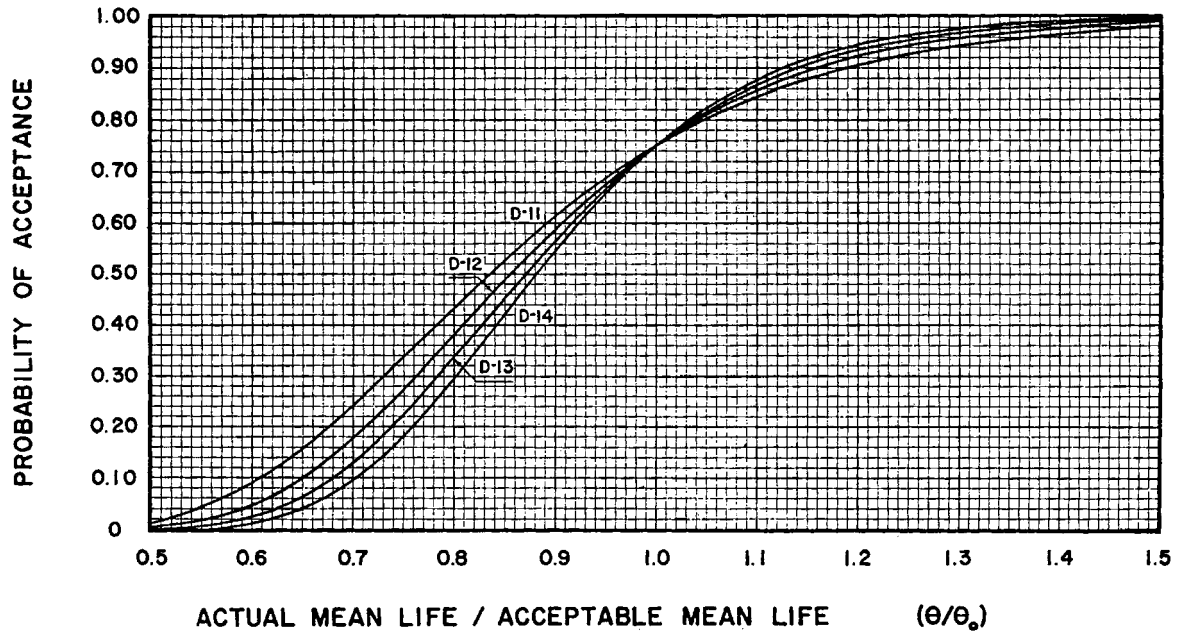


These curves are valid only when sampling from an exponential distribution.

Note: Notations on curves are sample plan code designation

FIG. A1.1 Operating Characteristic Curves for Life Tests Terminated Upon Occurrence of Preassigned Number of Failures (continued)

(Curves for sequential plans and tests terminated at pre-assigned time are essentially equivalent)

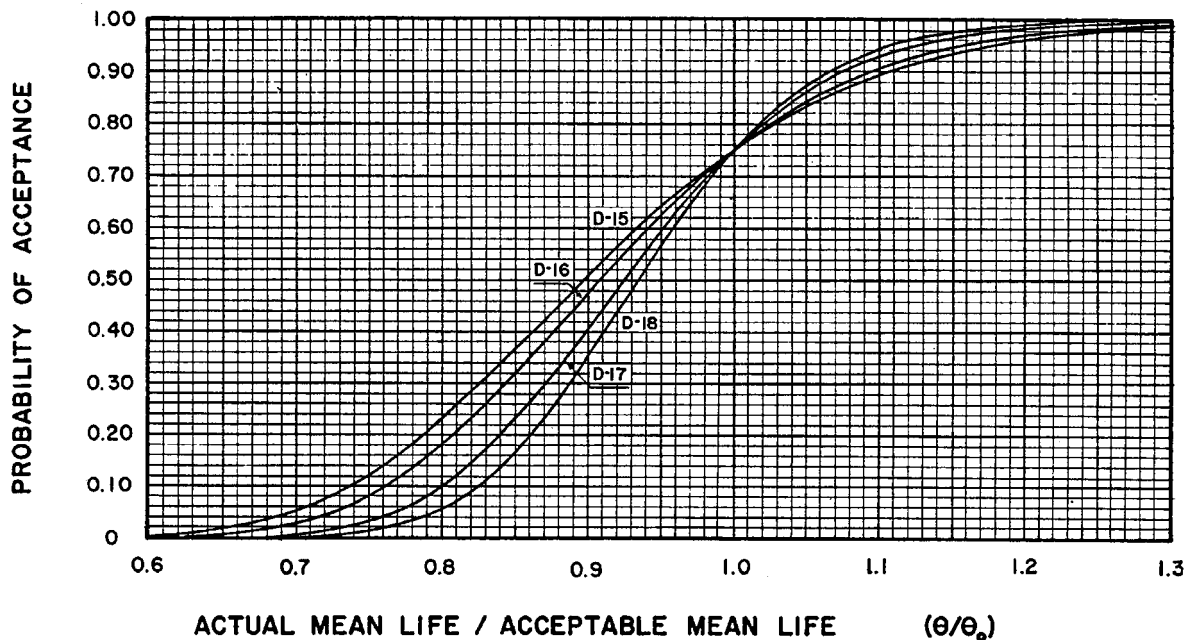


These curves are valid only when sampling from an exponential distribution.

Note: Notations on curves are sample plan code designation

FIG. A1.1 Operating Characteristic Curves for Life Tests Terminated Upon Occurrence of Preassigned Number of Failures (continued)

(Curves for sequential plans and tests terminated at pre-assigned time are essentially equivalent)

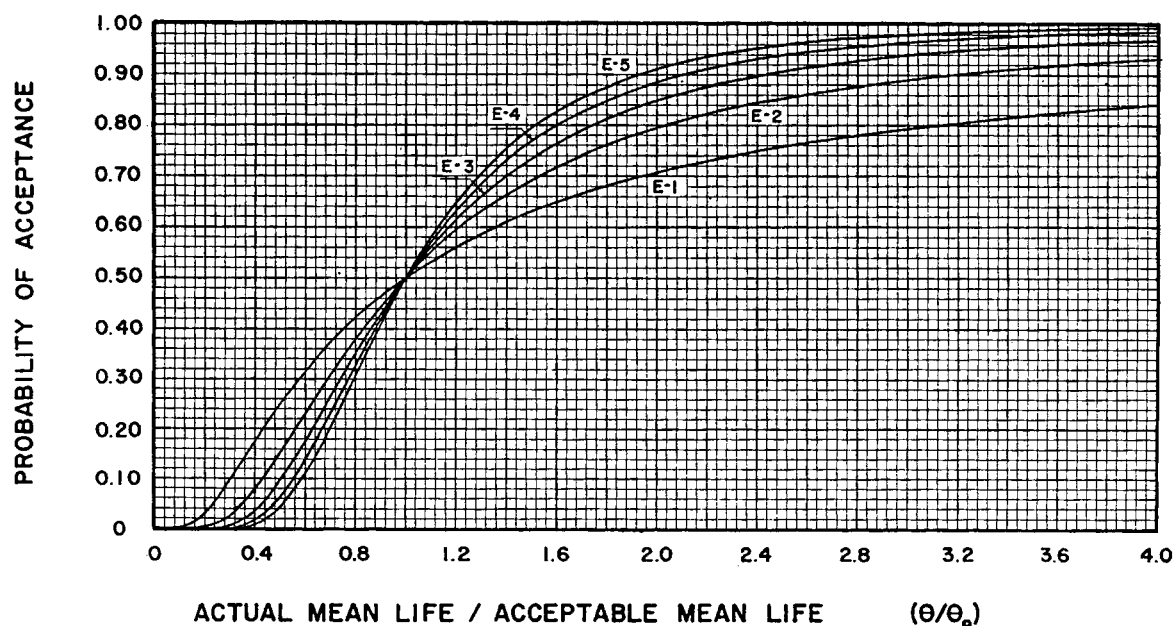


These curves are valid only when sampling from an exponential distribution.

Note: Notations on curves are sample plan code designation

FIG. A1.1 Operating Characteristic Curves for Life Tests Terminated Upon Occurrence of Preassigned Number of Failures (continued)

(Curves for sequential plans and tests terminated at pre-assigned time are essentially equivalent)

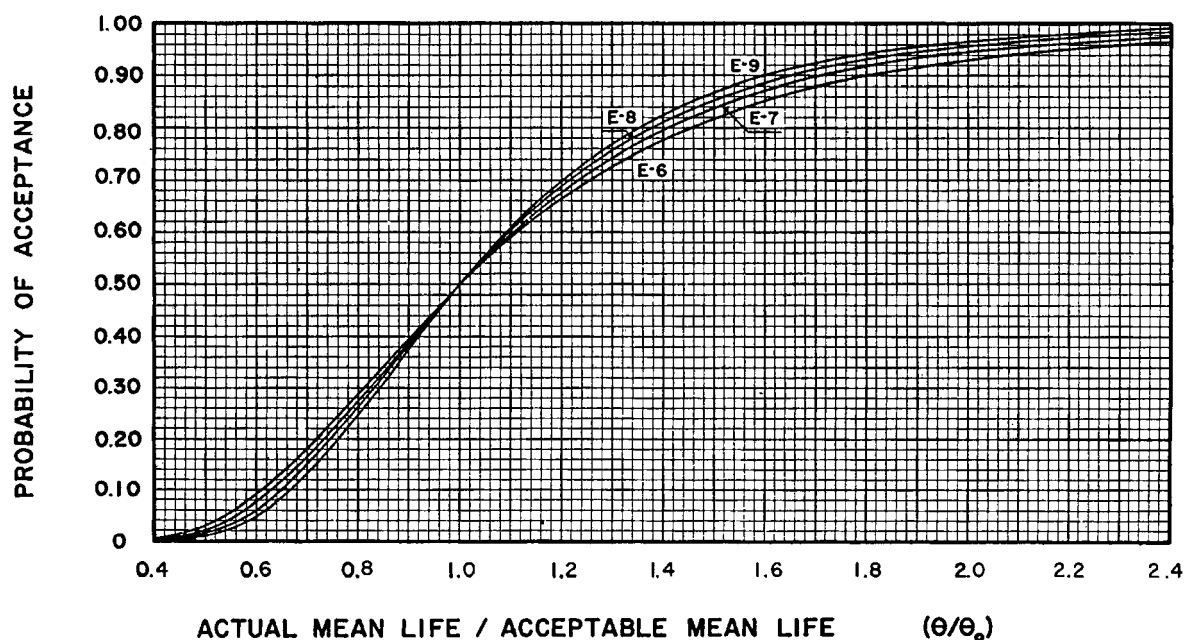


These curves are valid only when sampling from an exponential distribution.

Note: Notations on curves are sample plan code designation

FIG. A1.1 Operating Characteristic Curves for Life Tests Terminated Upon Occurrence of Preassigned Number of Failures (continued)

(Curves for sequential plans and tests terminated at pre-assigned time are essentially equivalent)

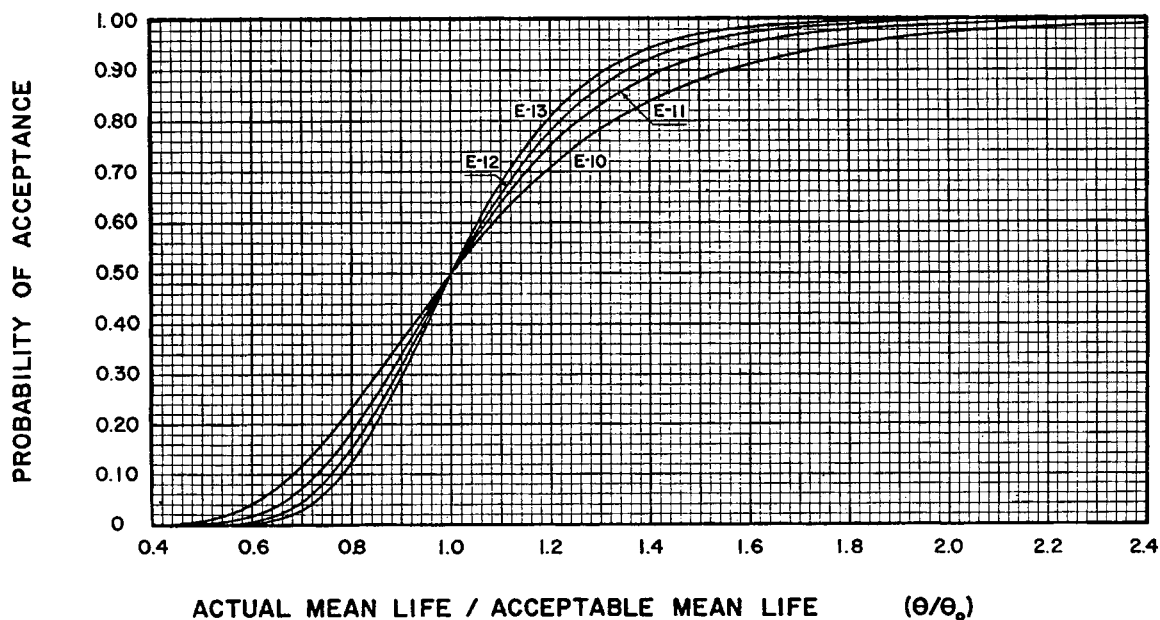


These curves are valid only when sampling from an exponential distribution.

Note: Notations on curves are sample plan code designation

FIG. A1.1 Operating Characteristic Curves for Life Tests Terminated Upon Occurrence of Preassigned Number of Failures (continued)

(Curves for sequential plans and tests terminated at pre-assigned time are essentially equivalent)

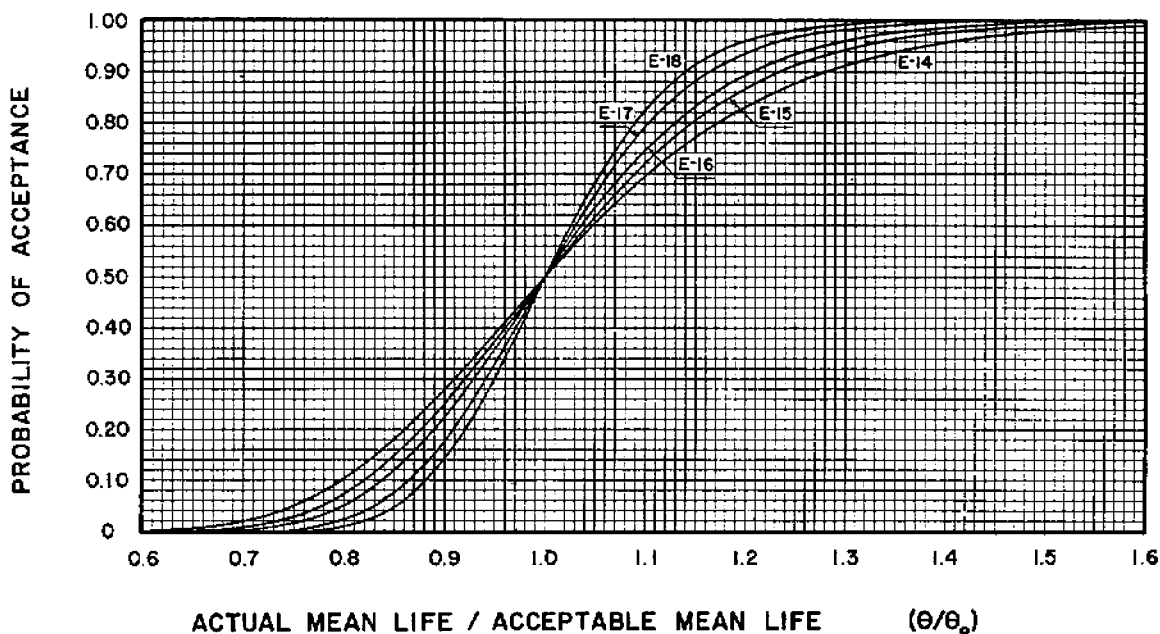


These curves are valid only when sampling from an exponential distribution.

Note: Notations on curves are sample plan code designation

FIG. A1.1 Operating Characteristic Curves for Life Tests Terminated Upon Occurrence of Preassigned Number of Failures (continued)

(Curves for sequential plans and tests terminated at pre-assigned time are essentially equivalent)



These curves are valid only when sampling from an exponential distribution.

Note: Notations on curves are sample plan code designation

FIG. A1.1 Operating Characteristic Curves for Life Tests Terminated Upon Occurrence of Preassigned Number of Failures (continued)

TABLE A1.2 Master Table for Life Tests Terminated Upon Occurrence of Preassigned Number of Failures

NOTE 1—Producer's risk α is the probability of rejecting lots with mean life θ_0 .

NOTE 2—Acceptance criterion: Accept lot if $\theta_{r,n} \geq \theta_0(C/\theta_0)$.

NOTE 3—For explanation of the code, see section 7.3.2 and Table A1.1.

r	Producer's Risk (α)									
	0.01		0.05		0.1		0.25		0.5	
	Code	C/θ_0	Code	C/θ_0	Code	C/θ_0	Code	C/θ_0	Code	C/θ_0
1	A-1	0.010	B-1	0.052	C-1	0.106	D-1	0.288	E-1	0.693
2	A-2	0.074	B-2	0.178	C-2	0.266	D-2	0.481	E-2	0.839
3	A-3	0.145	B-3	0.272	C-3	0.367	D-3	0.576	E-3	0.891
4	A-4	0.206	B-4	0.342	C-4	0.436	D-4	0.634	E-4	0.918
5	A-5	0.256	B-5	0.394	C-5	0.487	D-5	0.674	E-5	0.934
6	A-6	0.298	B-6	0.436	C-6	0.525	D-6	0.703	E-6	0.945
7	A-7	0.333	B-7	0.469	C-7	0.556	D-7	0.726	E-7	0.953
8	A-8	0.363	B-8	0.498	C-8	0.582	D-8	0.744	E-8	0.959
9	A-9	0.390	B-9	0.522	C-9	0.604	D-9	0.760	E-9	0.963
10	A-10	0.413	B-10	0.543	C-10	0.622	D-10	0.773	E-10	0.967
15	A-11	0.498	B-11	0.616	C-11	0.687	D-11	0.816	E-11	0.978
20	A-12	0.554	B-12	0.663	C-12	0.726	D-12	0.842	E-12	0.983
25	A-13	0.594	B-13	0.695	C-13	0.754	D-13	0.859	E-13	0.987
30	A-14	0.625	B-14	0.720	C-14	0.774	D-14	0.872	E-14	0.989
40	A-15	0.669	B-15	0.755	C-15	0.803	D-15	0.889	E-15	0.992
50	A-16	0.701	B-16	0.779	C-16	0.824	D-16	0.901	E-16	0.993
75	A-17	0.751	B-17	0.818	C-17	0.855	D-17	0.920	E-17	0.996
100	A-18	0.782	B-18	0.841	C-18	0.874	D-18	0.931	E-18	0.997

TABLE A1.3 Life Tests Terminated Upon Occurrence of Preassigned Number of Failures—Testing Without Replacement

NOTE 1—Expected waiting time values:

Expected waiting time for r failures in a sample of n
Mean life of lot

NOTE 2—In the table $r = 1(1)n$ and $n = 1(1)20(5)30(10)100$

r	n	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
1	1.0000	0.5000	0.3333	0.2500	0.2000	0.1667	0.1429	0.1250	0.1111	0.1000	0.0909	0.0833	0.0769	0.0714	0.0667	
2	1.5000	0.8333	0.5833	0.4500	0.3667	0.3095	0.2679	0.2361	0.2111	0.1909	0.1742	0.1603	0.1484	0.1381		
3	1.8333	1.0833	0.7833	0.6167	0.5095	0.4345	0.3790	0.3361	0.3020	0.2742	0.2512	0.2317	0.2150			
4	2.0833	1.2833	0.9500	0.7595	0.6345	0.5456	0.4790	0.4270	0.3854	0.3512	0.3226	0.2984				
5	2.2833	1.4500	1.0929	0.8845	0.7456	0.6456	0.5699	0.5104	0.4623	0.4226	0.3893					
6	2.4500	1.5929	1.2179	0.9956	0.8456	0.7365	0.6532	0.5873	0.5337	0.4893						
7	2.5929	1.7179	1.3290	1.0956	0.9365	0.8199	0.7301	0.6587	0.6004							
8	2.7179	1.8290	1.4290	1.1865	1.0199	0.8968	0.8016	0.7254								
9	2.8290	1.9290	1.5199	1.2699	1.0968	0.9682	0.8682									
10	2.9290	2.0199	1.6032	1.3468	1.1682	1.0349										
11	3.0199	2.1032	1.6801	1.4182	1.2349											
12	3.1032	2.1801	1.7516	1.4849												
13	3.1801	2.2516	1.8182													
14	3.2516	2.3182														
15	3.3182															

r	n	16	17	18	19	20	25	30	40	50	60	70	80	90	100
1	0.0625	0.0588	0.0556	0.0526	0.0500	0.0400	0.0333	0.0250	0.0200	0.0167	0.0143	0.0125	0.0111	0.0100	
2	0.1292	0.1213	0.1144	0.1082	0.1026	0.0817	0.0678	0.0506	0.0404	0.0336	0.0288	0.0252	0.0223	0.0201	
3	0.2006	0.1880	0.1769	0.1670	0.1582	0.1251	0.1035	0.0770	0.0612	0.0509	0.0435	0.0380	0.0337	0.0303	
4	0.2775	0.2594	0.2435	0.2295	0.2170	0.1706	0.1406	0.1040	0.0825	0.0684	0.0584	0.0510	0.0452	0.0406	
5	0.3609	0.3363	0.3150	0.2962	0.2795	0.2182	0.1790	0.1318	0.1043	0.0863	0.0736	0.0641	0.0568	0.0510	
6	0.4518	0.4197	0.3919	0.3676	0.3462	0.2682	0.2190	0.1603	0.1265	0.1044	0.0889	0.0775	0.0686	0.0616	
7	0.5518	0.5106	0.4752	0.4445	0.4176	0.3209	0.2607	0.1897	0.1492	0.1230	0.1046	0.0910	0.0805	0.0722	
8	0.6629	0.6106	0.5661	0.5279	0.4945	0.3764	0.3042	0.2200	0.1725	0.1418	0.1204	0.1047	0.0926	0.0829	
9	0.7879	0.7217	0.6661	0.6188	0.5779	0.4352	0.3496	0.2513	0.1963	0.1611	0.1366	0.1186	0.1047	0.0938	
10	0.9307	0.8467	0.7773	0.7188	0.6688	0.4977	0.3972	0.2836	0.2207	0.1807	0.1530	0.1326	0.1171	0.1048	
11	1.0974	0.9896	0.9023	0.8299	0.7688	0.5644	0.4472	0.3169	0.2457	0.2007	0.1696	0.1469	0.1296	0.1159	
12	1.2974	1.1562	1.0451	0.9549	0.8799	0.6358	0.4999	0.3514	0.2713	0.2211	0.1866	0.1614	0.1422	0.1272	
13	1.5474	1.3562	1.2118	1.0977	1.0049	0.7127	0.5554	0.3871	0.2976	0.2419	0.2038	0.1761	0.1551	0.1385	
14	1.8807	1.6062	1.4118	1.2644	1.1477	0.7961	0.6143	0.4241	0.3246	0.2632	0.2214	0.1911	0.1681	0.1500	
15	2.3807	1.9396	1.6618	1.4644	1.3144	0.8870	0.6768	0.4626	0.3524	0.2849	0.2392	0.2062	0.1812	0.1616	
16	3.3807	2.4396	1.9951	1.7144	1.5144	0.9870	0.7434	0.5026	0.3810	0.3071	0.2574	0.2216	0.1945	0.1734	
17	3.4396	2.4951	2.0477	1.7644	1.5644	1.0981	0.8149	0.5443	0.4104	0.3299	0.2759	0.2372	0.2081	0.1853	
18	3.4951	2.5477	2.0977	1.8231	1.6231	1.2231	0.8918	0.5877	0.4407	0.3531	0.2948	0.2531	0.2218	0.1974	
19	3.5477	2.5977	2.1477	1.8731	1.6731	1.2731	0.9418	0.6332	0.4720	0.3769	0.3140	0.2692	0.2356	0.2096	
20	3.5977	2.6477	2.1977	1.9231	1.7231	1.3231	0.9918	0.6808	0.5042	0.4013	0.3336	0.2856	0.2497	0.2219	
21	1.7326	1.1660	0.7308	0.5376	0.4263	0.3536	0.3023	0.2640	0.2344						
22	1.9826	1.2771	0.7834	0.5720	0.4520	0.3740	0.3192	0.2785	0.2471						
23	2.3160	1.4021	0.8390	0.6077	0.4783	0.3949	0.3365	0.2932	0.2599						
24	2.8160	1.5450	0.8978	0.6448	0.5053	0.4161	0.3540	0.3081	0.2729						
25	3.8160	1.7117	0.9603	0.6832	0.5331	0.4379	0.3719	0.3233	0.2860						
26	1.9117	1.0270	0.7232	0.5617	0.4601	0.3900	0.3387	0.2994							
27	2.1617	1.0984	0.7649	0.5911	0.4828	0.4086	0.3543	0.3129							
28	2.4950	1.1753	0.8084	0.6214	0.5061	0.4274	0.3702	0.3266							
29	2.9950	1.2587	0.8538	0.6526	0.5299	0.4467	0.3863	0.3405							
30	3.9950	1.3496	0.9015	0.6849	0.5543	0.4663	0.4027	0.3545							
31	1.4496	0.9515	0.7182	0.5793	0.4863	0.4194	0.3688								
32	1.5607	1.0041	0.7527	0.6049	0.5067	0.4363	0.3833								
33	1.6857	1.0597	0.7884	0.6313	0.5275	0.4536	0.3980								
34	1.8285	1.1185	0.8255	0.6583	0.5488	0.4711	0.4130								
35	1.9952	1.1810	0.8639	0.6861	0.5705	0.4890	0.4281								
36	2.1952	1.2476	0.9039	0.7146	0.5928	0.5071	0.4435								
37	2.4452	1.3191	0.9456	0.7440	0.6155	0.5257	0.4591								
38	2.7785	1.3960	0.9891	0.7743	0.6387	0.5445	0.4750								
39	3.2785	1.4793	1.0345	0.8056	0.6625	0.5638	0.4911								
40	4.2785	1.5702	1.0821	0.8378	0.6869	0.5834	0.5075								
41	1.6702	1.1321	0.8712	0.7119	0.6034	0.5242									
42	1.7813	1.1848	0.9057	0.7376	0.6238	0.5411									
43	1.9063	1.2403	0.9414	0.7639	0.6446	0.5584									
44	2.0492	1.2991	0.9784	0.7909	0.6659	0.5759									
45	2.2159	1.3616	1.0169	0.8187	0.6876	0.5938									
46	2.4159	1.4283	1.0569	0.8473	0.7098	0.6119									
47	2.6659	1.4997	1.0985	0.8767	0.7326	0.6305									

TABLE A1.3 *Continued*

r	n														
	16	17	18	19	20	25	30	40	50	60	70	80	90	100	
48									2.9992	1.5767	1.1420	0.9070	0.7558	0.6493	
49									3.4992	1.6600	1.1875	0.9382	0.7796	0.6686	
50									4.4992	1.7509	1.2351	0.9705	0.8040	0.6882	
51										1.8509	1.2851	1.0038	0.8290	0.7082	
52										1.9620	1.3377	1.0383	0.8547	0.7286	
53										2.0870	1.3933	1.0740	0.8810	0.7494	
54										2.2299	1.4521	1.1111	0.9080	0.7707	
55										2.3965	1.5146	1.1495	0.9358	0.7924	
56										2.5965	1.5813	1.1895	0.9644	0.8147	
57										2.8465	1.6527	1.2312	0.9938	0.8374	
58										3.1799	1.7296	1.2747	1.0241	0.8606	
59										3.6799	1.8130	1.3201	1.0553	0.8844	
60										4.6799	1.9039	1.3677	1.0876	0.9088	
61											2.0039	1.4177	1.1209	0.9338	
62											2.1150	1.4704	1.1554	0.9595	
63											2.2400	1.5259	1.1911	0.9858	
64											2.3828	1.5848	1.2282	1.0128	
65											2.5495	1.6473	1.2666	1.0406	
66											2.7495	1.7139	1.3066	1.0692	
67											2.9995	1.7853	1.3483	1.0986	
68											3.3328	1.8623	1.3918	1.1289	
69											3.8328	1.9456	1.4372	1.1601	
70											4.8328	2.0365	1.4848	1.1924	
71												2.1365	1.5348	1.2257	
72												2.2476	1.5875	1.2602	
73												2.3726	1.6430	1.2959	
74												2.5155	1.7018	1.3330	
75												2.6821	1.7643	1.3714	
76												2.8821	1.8310	1.4114	
77												3.1321	1.9024	1.4531	
78												3.4655	1.9794	1.4966	
79												3.9655	2.0627	1.5420	
80												4.9655	2.1536	1.5896	
81													2.2536	1.6396	
82													2.3647	1.6923	
83													2.4897	1.7478	
84													2.6326	1.8066	
85													2.7992	1.8691	
86													2.9992	1.9358	
87													3.2492	2.0072	
88													3.5826	2.0842	
89													4.0826	2.1675	
90													5.0826	2.2584	
91														2.3584	
92														2.4695	
93														2.5945	
94														2.7374	
95														2.9040	
96														3.1040	
97														3.3540	
98														3.6874	
99														4.1874	
100														5.1874	

TABLE A1.4 Life Tests Terminated Upon Occurrence of Preassigned Number of Failures—Testing Without Replacement

NOTE 1—Expected waiting time values:

$$\frac{\text{Expected waiting time for } r \text{ failures in a sample of } n}{\text{Mean life of lot}}$$

NOTE 2—In the table $r = 1(1)10(5)30(10)50(25)100$ and $n = kr$, with $k = 1(1)10(10)20$

	n											
r		r	2r	3r	4r	5r	6r	7r	8r	9r	10r	20r
1		1.0000	0.5000	0.3333	0.2500	0.2000	0.1667	0.1429	0.1250	0.1111	0.1000	0.0500
2		1.5000	0.5833	0.3667	0.2679	0.2111	0.1742	0.1484	0.1292	0.1144	0.1026	0.0506
3		1.8333	0.6167	0.3790	0.2742	0.2150	0.1769	0.1503	0.1306	0.1155	0.1035	0.0509
4		2.0833	0.6345	0.3854	0.2775	0.2170	0.1782	0.1512	0.1313	0.1161	0.1040	0.0510
5		2.2833	0.6456	0.3893	0.2795	0.2182	0.1790	0.1518	0.1318	0.1164	0.1043	0.0510
6		2.4500	0.6532	0.3919	0.2809	0.2190	0.1796	0.1522	0.1321	0.1166	0.1044	0.0511
7		2.5929	0.6587	0.3938	0.2818	0.2196	0.1800	0.1525	0.1323	0.1168	0.1046	0.0511
8		2.7179	0.6629	0.3952	0.2825	0.2200	0.1803	0.1527	0.1324	0.1169	0.1047	0.0511
9		2.8290	0.6661	0.3963	0.2831	0.2204	0.1805	0.1528	0.1325	0.1170	0.1047	0.0511
10		2.9290	0.6688	0.3972	0.2836	0.2207	0.1807	0.1530	0.1326	0.1171	0.1048	0.0512
15		3.3182	0.6768	0.4000	0.2849	0.2215	0.1812	0.1534	0.1329	0.1173	0.1050	0.0512
20		3.5977	0.6808	0.4013	0.2856	0.2219	0.1815	0.1536	0.1331	0.1174	0.1051	0.0512
25		3.8160	0.6832	0.4022	0.2860	0.2221	0.1817	0.1537	0.1332	0.1175	0.1051	0.0512
30		3.9950	0.6849	0.4027	0.2863	0.2223	0.1818	0.1538	0.1332	0.1176	0.1052	0.0512
40		4.2785	0.6869	0.4034	0.2866	0.2225	0.1819	0.1539	0.1333	0.1176	0.1052	0.0513
50		4.4992	0.6882	0.4038	0.2869	0.2226	0.1820	0.1539	0.1334	0.1176	0.1052	0.0513
75		4.9014	0.6898	0.4044	0.2871	0.2228	0.1821	0.1540	0.1334	0.1177	0.1053	0.0513
100		5.1874	0.6907	0.4046	0.2873	0.2229	0.1822	0.1540	0.1334	0.1177	0.1053	0.0513

TABLE A1.5 Expected Relative Saving in Time by Increasing Sample Size

NOTE 1—The values tabled here are the ratios:

$$\frac{\text{Expected waiting time for } r \text{ failures in a sample of } n}{\text{Expected waiting time for } r \text{ failures in a sample of } r}$$

NOTE 2—For any given value of r , the smaller the tabled value, the greater is the relative expected saving in time. Thus, increasing the sample size will decrease the expected waiting time required for decision.

n		1	2	3	4	5	10	15	20
r									
1	1	1.000	0.500	0.333	0.250	0.200	0.100	0.067	0.050
	2		1.000	0.556	0.389	0.300	0.141	0.092	0.068
	3			1.000	0.591	0.427	0.183	0.117	0.086
	4				1.000	0.616	0.230	0.143	0.104
	5					1.000	0.283	0.170	0.122
	10						1.000	0.353	0.228

TABLE A1.6 Expected Relative Saving in Time by Testing With Replacement

NOTE 1—The values tabled here are the ratios:

$$\frac{\text{Expected waiting time for } r \text{ failures in a sample of } n \text{ when testing with replacement}}{\text{Expected waiting time for } r \text{ failures in a sample of } n \text{ when testing without replacement}}$$

NOTE 2—For any given value of r , the smaller the tabled value, the greater is the relative expected saving in time. Thus, as the sample size increases, replacing failed units result in decreasing relative saving in time. It should be noted that the time saved by replacing failures is at a cost of having placed more units of product on test.

r	Sample Size							
	1	2	3	4	5	10	15	20
1	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00
2		0.67	0.80	0.86	0.89	0.95	0.97	0.97
3			0.55	0.69	0.77	0.89	0.93	0.95
4				0.48	0.62	0.84	0.89	0.92
5					0.44	0.77	0.86	0.89
10						0.34	0.64	0.75

TABLE A1.7 Life Test Sampling Plans for Specified α , β , θ_1/θ_0

NOTE—A complete set of OC curves is not provided for the sampling plans of this table. For those sampling plans marked (*), the appropriate OC curves in Fig. A1.1 may be used by determining, from Table A1.2, the sample code designation corresponding to the same values of α and r . For the sampling plans that are not marked (*), two points $(1, 1-\alpha)$ and $(\theta_1/\theta_0, \beta)$ on the OC curves are given.

θ_1/θ_0	$\alpha = 0.01$		$\alpha = 0.01$		$\alpha = 0.01$		$\alpha = 0.01$	
	$\beta = 0.01$		$\beta = 0.05$		$\beta = 0.10$		$\beta = 0.25$	
	r	C/ θ_0	r	C/ θ_0	r	C/ θ_0	r	C/ θ_0
2/3	136	0.811	101	0.783	83	0.762	60	0.724
1/2	46	0.689	35	0.649	30*	0.625	22	0.572
1/3	19	0.545	15*	0.498	13	0.469	10*	0.413
1/5	9*	0.390	8*	0.363	7*	0.333	5*	0.256
1/10	5*	0.256	4*	0.206	4*	0.206	3*	0.145
θ_1/θ_0	$\alpha = 0.05$		$\alpha = 0.05$		$\alpha = 0.05$		$\alpha = 0.05$	
	$\beta = 0.01$		$\beta = 0.05$		$\beta = 0.10$		$\beta = 0.25$	
	r	C/ θ_0	r	C/ θ_0	r	C/ θ_0	r	C/ θ_0
2/3	95	0.837	67	0.808	55	0.789	35	0.739
1/2	33	0.732	23	0.683	19	0.655	13	0.592
1/3	13	0.592	10*	0.543	8*	0.498	6*	0.436
1/5	7*	0.469	5*	0.394	4*	0.342	3*	0.273
1/10	4*	0.342	3*	0.273	3*	0.273	2*	0.178
θ_1/θ_0	$\alpha = 0.10$		$\alpha = 0.10$		$\alpha = 0.10$		$\alpha = 0.10$	
	$\beta = 0.01$		$\beta = 0.05$		$\beta = 0.10$		$\beta = 0.25$	
	r	C/ θ_0	r	C/ θ_0	r	C/ θ_0	r	C/ θ_0
2/3	77	0.857	52	0.827	41	0.806	25*	0.754
1/2	26	0.758	18	0.712	15*	0.687	9*	0.604
1/3	11	0.638	8*	0.582	6*	0.525	4*	0.436
1/5	5*	0.487	4*	0.436	3*	0.367	3*	0.367
1/10	3*	0.367	2*	0.266	2*	0.266	2*	0.266
θ_1/θ_0	$\alpha = 0.01$		$\alpha = 0.01$		$\alpha = 0.01$		$\alpha = 0.01$	
	$\beta = 0.01$		$\beta = 0.05$		$\beta = 0.10$		$\beta = 0.25$	
	r	C/ θ_0	r	C/ θ_0	r	C/ θ_0	r	C/ θ_0
2/3	52	0.903	32	0.876	23	0.853	12	0.793
1/2	17	0.828	11	0.784	8*	0.745	5*	0.674
1/3	7*	0.726	5*	0.674	4*	0.634	2*	0.481
1/5	3*	0.576	2*	0.481	2*	0.481	1*	0.288
1/10	2*	0.481	2*	0.481	1*	0.288	1*	0.288

TABLE A1.8 Master Table for Life Tests Terminated at Preassigned Time—Testing Without Replacement

NOTE—For explanation of the code, see section 7.3.2 and Table A1.1.

Values of T/θ_0 for $\alpha = 0.01$											
Code	r	Sample Size									
		$2r$	$3r$	$4r$	$5r$	$6r$	$7r$	$8r$	$9r$	$10r$	$20r$
A-1	1	0.005	0.003	0.003	0.002	0.002	0.001	0.001	0.001	0.001	0.0005
A-2	2	0.043	0.027	0.020	0.016	0.013	0.011	0.010	0.008	0.008	0.004
A-3	3	0.089	0.055	0.040	0.031	0.026	0.022	0.019	0.017	0.015	0.007
A-4	4	0.131	0.079	0.057	0.045	0.037	0.031	0.027	0.024	0.021	0.011
A-5	5	0.165	0.100	0.072	0.056	0.046	0.039	0.034	0.030	0.027	0.013
A-6	6	0.195	0.117	0.084	0.065	0.054	0.045	0.039	0.035	0.031	0.015
A-7	7	0.219	0.131	0.094	0.073	0.060	0.051	0.044	0.039	0.035	0.017
A-8	8	0.241	0.143	0.103	0.080	0.065	0.055	0.048	0.042	0.038	0.019
A-9	9	0.260	0.155	0.110	0.086	0.070	0.060	0.052	0.046	0.041	0.020
A-10	10	0.276	0.164	0.117	0.091	0.075	0.063	0.055	0.048	0.043	0.021
A-11	15	0.337	0.199	0.142	0.110	0.090	0.076	0.066	0.058	0.052	0.025
A-12	20	0.377	0.222	0.158	0.123	0.101	0.085	0.074	0.065	0.058	0.028
A-13	25	0.406	0.239	0.170	0.132	0.108	0.091	0.079	0.070	0.062	0.030
A-14	30	0.428	0.252	0.179	0.139	0.114	0.096	0.083	0.074	0.066	0.032
A-15	40	0.460	0.270	0.192	0.149	0.122	0.103	0.089	0.079	0.070	0.034
A-16	50	0.482	0.283	0.201	0.156	0.128	0.108	0.094	0.082	0.074	0.036
A-17	75	0.518	0.304	0.216	0.167	0.137	0.116	0.100	0.088	0.079	0.039
A-18	100	0.540	0.316	0.225	0.174	0.142	0.120	0.104	0.092	0.082	0.040

TABLE A1.9 Master Table for Life Tests Terminated at Preassigned Time—Testing Without Replacement

NOTE—For explanation of the code, see section 7.3.2 and Table A1.1.

Values of T/θ_0 for $\alpha = 0.05$											
Code	r	Sample Size									
		2r	3r	4r	5r	6r	7r	8r	9r	10r	20r
B-1	1	0.026	0.017	0.013	0.010	0.009	0.007	0.006	0.006	0.005	0.003
B-2	2	0.104	0.065	0.048	0.038	0.031	0.026	0.023	0.020	0.018	0.009
B-3	3	0.168	0.103	0.075	0.058	0.048	0.041	0.036	0.031	0.023	0.014
B-4	4	0.217	0.132	0.095	0.074	0.061	0.052	0.045	0.040	0.036	0.017
B-5	5	0.254	0.153	0.110	0.086	0.071	0.060	0.052	0.046	0.041	0.020
B-6	6	0.284	0.170	0.122	0.095	0.078	0.066	0.057	0.051	0.045	0.022
B-7	7	0.309	0.185	0.132	0.103	0.084	0.072	0.062	0.053	0.049	0.024
B-8	8	0.330	0.197	0.141	0.110	0.090	0.078	0.066	0.058	0.052	0.025
B-9	9	0.348	0.207	0.148	0.115	0.094	0.080	0.069	0.061	0.053	0.027
B-10	10	0.363	0.216	0.154	0.120	0.098	0.083	0.072	0.064	0.057	0.028
B-11	15	0.417	0.246	0.175	0.136	0.112	0.094	0.082	0.072	0.063	0.032
B-12	20	0.451	0.266	0.189	0.147	0.120	0.102	0.088	0.078	0.070	0.034
B-13	25	0.475	0.280	0.199	0.154	0.126	0.107	0.093	0.082	0.073	0.036
B-14	30	0.493	0.290	0.206	0.160	0.131	0.111	0.096	0.085	0.076	0.037
B-15	40	0.519	0.305	0.216	0.168	0.137	0.116	0.101	0.089	0.079	0.039
B-16	50	0.536	0.315	0.223	0.173	0.142	0.120	0.104	0.092	0.082	0.040
B-17	75	0.564	0.331	0.235	0.182	0.149	0.126	0.109	0.096	0.086	0.042
B-18	100	0.581	0.340	0.242	0.187	0.153	0.130	0.112	0.099	0.089	0.043

TABLE A1.10 Master Table for Life Tests Terminated at Preassigned Time—Testing Without Replacement

NOTE—For explanation of the code, see section 7.3.2 and Table A1.1.

Values of T/θ_0 for $\alpha = 0.10$											
Code	r	Sample Size									
		2r	3r	4r	5r	6r	7r	8r	9r	10r	20r
C-1	1	0.053	0.035	0.026	0.021	0.018	0.015	0.013	0.012	0.011	0.005
C-2	2	0.155	0.098	0.071	0.056	0.046	0.039	0.034	0.030	0.027	0.013
C-3	3	0.226	0.139	0.101	0.079	0.065	0.055	0.048	0.042	0.038	0.019
C-4	4	0.277	0.168	0.121	0.095	0.078	0.066	0.057	0.051	0.045	0.022
C-5	5	0.314	0.189	0.136	0.106	0.087	0.074	0.064	0.057	0.051	0.025
C-6	6	0.343	0.206	0.147	0.115	0.094	0.080	0.069	0.061	0.055	0.027
C-7	7	0.366	0.219	0.157	0.122	0.100	0.085	0.074	0.065	0.058	0.028
C-8	8	0.386	0.230	0.164	0.128	0.105	0.089	0.077	0.068	0.061	0.030
C-9	9	0.402	0.239	0.171	0.133	0.109	0.092	0.080	0.071	0.063	0.031
C-10	10	0.416	0.247	0.176	0.137	0.112	0.095	0.082	0.073	0.065	0.032
C-11	15	0.465	0.275	0.196	0.152	0.124	0.105	0.091	0.081	0.072	0.035
C-12	20	0.494	0.291	0.207	0.161	0.132	0.112	0.097	0.085	0.076	0.037
C-13	25	0.515	0.303	0.216	0.167	0.137	0.116	0.100	0.089	0.079	0.039
C-14	30	0.530	0.312	0.222	0.172	0.141	0.119	0.103	0.091	0.081	0.040
C-15	40	0.552	0.324	0.230	0.179	0.146	0.124	0.107	0.094	0.084	0.041
C-16	50	0.567	0.333	0.236	0.183	0.150	0.127	0.110	0.097	0.087	0.042
C-17	75	0.590	0.346	0.245	0.190	0.156	0.132	0.114	0.101	0.090	0.044
C-18	100	0.604	0.354	0.251	0.195	0.159	0.135	0.117	0.103	0.092	0.045

TABLE A1.11 Master Table for Life Tests Terminated at Preassigned Time—Testing Without Replacement

NOTE—For explanation of the code, see section 7.3.2 and Table A1.1.

Values of T/θ_0 for $\alpha = 0.25$											
Code	r	Sample Size									
		2r	3r	4r	5r	6r	7r	8r	9r	10r	20r
D-1	1	0.144	0.096	0.072	0.058	0.048	0.041	0.036	0.032	0.029	0.014
D-2	2	0.281	0.176	0.129	0.102	0.084	0.071	0.062	0.055	0.049	0.024
D-3	3	0.355	0.218	0.158	0.124	0.102	0.087	0.075	0.067	0.060	0.029
D-4	4	0.402	0.244	0.176	0.138	0.113	0.096	0.083	0.074	0.066	0.032
D-5	5	0.435	0.262	0.188	0.147	0.123	0.102	0.089	0.078	0.070	0.034
D-6	6	0.459	0.276	0.197	0.154	0.126	0.107	0.093	0.082	0.073	0.036
D-7	7	0.478	0.286	0.205	0.159	0.131	0.111	0.096	0.085	0.076	0.037
D-8	8	0.493	0.294	0.210	0.164	0.134	0.114	0.099	0.087	0.078	0.038
D-9	9	0.506	0.301	0.215	0.168	0.137	0.116	0.101	0.089	0.080	0.039
D-10	10	0.517	0.307	0.219	0.171	0.140	0.118	0.102	0.091	0.081	0.040
D-11	15	0.552	0.326	0.232	0.181	0.148	0.125	0.108	0.096	0.086	0.042
D-12	20	0.573	0.338	0.240	0.187	0.153	0.129	0.112	0.099	0.088	0.043
D-13	25	0.587	0.345	0.246	0.191	0.156	0.132	0.114	0.101	0.090	0.044
D-14	30	0.597	0.351	0.250	0.194	0.159	0.134	0.116	0.103	0.092	0.045
D-15	40	0.611	0.359	0.255	0.198	0.162	0.137	0.119	0.105	0.094	0.046
D-16	50	0.620	0.364	0.258	0.201	0.164	0.139	0.120	0.106	0.095	0.046
D-17	75	0.635	0.372	0.264	0.205	0.168	0.142	0.123	0.108	0.097	0.047
D-18	100	0.643	0.377	0.267	0.208	0.170	0.143	0.124	0.110	0.098	0.048

TABLE A1.12 Master Table for Life Tests Terminated at Preassigned Time—Testing Without Replacement

NOTE—For explanation of the code, see section 7.3.2 and Table A1.1.

Values of T/θ_0 for $\alpha = 0.50$											
Code	r	Sample Size									
		2r	3r	4r	5r	6r	7r	8r	9r	10r	20r
E-1	1	0.346	0.231	0.173	0.139	0.116	0.099	0.087	0.077	0.069	0.035
E-2	2	0.489	0.308	0.225	0.177	0.146	0.125	0.108	0.096	0.086	0.042
E-3	3	0.549	0.338	0.244	0.192	0.158	0.134	0.116	0.103	0.092	0.045
E-4	4	0.582	0.354	0.255	0.199	0.164	0.139	0.121	0.107	0.095	0.047
E-5	5	0.603	0.364	0.261	0.204	0.167	0.142	0.123	0.109	0.097	0.048
E-6	6	0.617	0.370	0.265	0.207	0.170	0.144	0.125	0.110	0.099	0.048
E-7	7	0.628	0.375	0.269	0.209	0.172	0.145	0.126	0.111	0.100	0.049
E-8	8	0.636	0.379	0.271	0.211	0.173	0.146	0.127	0.112	0.100	0.049
E-9	9	0.641	0.382	0.273	0.212	0.174	0.147	0.128	0.113	0.101	0.049
E-10	10	0.647	0.384	0.274	0.213	0.175	0.148	0.128	0.113	0.101	0.050
E-11	15	0.662	0.391	0.279	0.217	0.177	0.150	0.130	0.115	0.103	0.050
E-12	20	0.669	0.394	0.281	0.218	0.178	0.151	0.131	0.115	0.103	0.050
E-13	25	0.674	0.397	0.282	0.219	0.179	0.152	0.131	0.116	0.104	0.051
E-14	30	0.677	0.398	0.283	0.220	0.180	0.152	0.132	0.116	0.104	0.051
E-15	40	0.681	0.400	0.284	0.221	0.180	0.153	0.132	0.117	0.104	0.051
E-16	50	0.683	0.401	0.285	0.221	0.181	0.153	0.132	0.117	0.104	0.051
E-17	75	0.687	0.403	0.286	0.222	0.181	0.153	0.133	0.117	0.105	0.051
E-18	100	0.689	0.403	0.286	0.222	0.182	0.154	0.133	0.117	0.105	0.051

TABLE A1.13 Master Table for Life Tests Terminated at Preassigned Time—Testing With Replacement

NOTE—For explanation of the code, see section 7.3.2 and Table A1.1.

Values of T/θ_0 for $\alpha = 0.01$

Code	r	Sample Size									
		2r	3r	4r	5r	6r	7r	8r	9r	10r	20r
A-1	1	0.005	0.003	0.003	0.002	0.002	0.001	0.001	0.001	0.001	0.0005
A-2	2	0.037	0.025	0.019	0.015	0.012	0.011	0.009	0.008	0.007	0.004
A-3	3	0.073	0.048	0.036	0.029	0.024	0.021	0.018	0.016	0.015	0.007
A-4	4	0.103	0.069	0.051	0.041	0.034	0.029	0.026	0.023	0.021	0.010
A-5	5	0.128	0.085	0.064	0.051	0.043	0.037	0.032	0.028	0.026	0.013
A-6	6	0.149	0.099	0.074	0.060	0.050	0.043	0.037	0.033	0.030	0.015
A-7	7	0.166	0.111	0.083	0.067	0.055	0.048	0.042	0.037	0.033	0.017
A-8	8	0.182	0.121	0.091	0.073	0.061	0.052	0.045	0.040	0.036	0.018
A-9	9	0.195	0.130	0.097	0.078	0.065	0.056	0.049	0.043	0.039	0.019
A-10	10	0.207	0.138	0.103	0.083	0.069	0.059	0.052	0.046	0.041	0.021
A-11	15	0.249	0.166	0.125	0.100	0.083	0.071	0.062	0.055	0.050	0.025
A-12	20	0.277	0.185	0.139	0.111	0.092	0.079	0.069	0.062	0.055	0.028
A-13	25	0.297	0.198	0.149	0.119	0.099	0.085	0.074	0.066	0.059	0.030
A-14	30	0.312	0.208	0.156	0.125	0.104	0.089	0.078	0.069	0.062	0.031
A-15	40	0.335	0.223	0.167	0.134	0.112	0.096	0.084	0.074	0.067	0.033
A-16	50	0.350	0.234	0.175	0.140	0.117	0.100	0.088	0.078	0.070	0.035
A-17	75	0.376	0.250	0.188	0.150	0.125	0.107	0.094	0.083	0.075	0.038
A-18	100	0.391	0.261	0.196	0.156	0.130	0.112	0.098	0.087	0.078	0.039

TABLE A1.14 Master Table for Life Tests Terminated at Preassigned Time—Testing With Replacement

NOTE—For explanation of the code, see section 7.3.2 and Table A1.1.

Values of T/θ_0 for $\alpha = 0.05$

Code	r	Sample Size									
		2r	3r	4r	5r	6r	7r	8r	9r	10r	20r
B-1	1	0.024	0.017	0.013	0.010	0.009	0.007	0.006	0.006	0.005	0.003
B-2	2	0.089	0.059	0.044	0.036	0.030	0.025	0.022	0.020	0.018	0.009
B-3	3	0.136	0.091	0.068	0.055	0.045	0.039	0.034	0.030	0.027	0.014
B-4	4	0.171	0.114	0.085	0.068	0.057	0.049	0.043	0.038	0.034	0.017
B-5	5	0.197	0.131	0.099	0.079	0.066	0.056	0.049	0.044	0.039	0.020
B-6	6	0.218	0.145	0.109	0.087	0.073	0.062	0.054	0.048	0.044	0.022
B-7	7	0.235	0.156	0.117	0.094	0.078	0.067	0.059	0.052	0.047	0.023
B-8	8	0.149	0.166	0.124	0.100	0.083	0.071	0.062	0.055	0.050	0.025
B-9	9	0.261	0.174	0.130	0.104	0.087	0.075	0.065	0.051	0.052	0.026
B-10	10	0.271	0.181	0.136	0.109	0.090	0.078	0.068	0.060	0.054	0.027
B-11	15	0.308	0.205	0.154	0.123	0.103	0.088	0.077	0.068	0.062	0.031
B-12	20	0.331	0.221	0.166	0.133	0.110	0.095	0.083	0.074	0.066	0.033
B-13	25	0.348	0.232	0.174	0.139	0.116	0.099	0.087	0.077	0.070	0.035
B-14	30	0.360	0.240	0.180	0.144	0.120	0.103	0.090	0.080	0.072	0.036
B-15	40	0.377	0.252	0.189	0.151	0.126	0.108	0.094	0.084	0.075	0.038
B-16	50	0.390	0.260	0.195	0.156	0.130	0.111	0.097	0.087	0.078	0.039
B-17	75	0.409	0.273	0.204	0.164	0.136	0.117	0.102	0.091	0.082	0.041
B-18	100	0.421	0.280	0.210	0.168	0.140	0.120	0.105	0.093	0.084	0.042

TABLE A1.15 Master Table for Life Tests Terminated at Preassigned Time—Testing With Replacement

NOTE—For explanation of the code, see section 7.3.2 and Table A1.1.

Values of T/θ_0 for $\alpha = 0.10$											
Code	r	Sample Size									
		2r	3r	4r	5r	6r	7r	8r	9r	10r	20r
A-1	1	0.053	0.035	0.026	0.021	0.018	0.015	0.013	0.012	0.011	0.005
A-2	2	0.133	0.089	0.066	0.053	0.044	0.038	0.033	0.030	0.027	0.013
A-3	3	0.184	0.122	0.092	0.073	0.061	0.052	0.046	0.041	0.037	0.018
A-4	4	0.218	0.145	0.109	0.087	0.073	0.062	0.055	0.048	0.044	0.022
A-5	5	0.243	0.162	0.122	0.097	0.081	0.070	0.061	0.054	0.049	0.024
A-6	6	0.263	0.175	0.131	0.105	0.088	0.075	0.066	0.058	0.053	0.026
A-7	7	0.278	0.185	0.139	0.111	0.093	0.079	0.070	0.062	0.056	0.028
A-8	8	0.291	0.194	0.146	0.116	0.097	0.083	0.073	0.065	0.058	0.029
A-9	9	0.302	0.201	0.151	0.121	0.101	0.086	0.075	0.067	0.060	0.030
A-10	10	0.311	0.207	0.156	0.124	0.104	0.089	0.078	0.069	0.062	0.031
A-11	15	0.343	0.229	0.172	0.137	0.114	0.091	0.086	0.076	0.065	0.034
A-12	20	0.363	0.242	0.182	0.145	0.121	0.104	0.091	0.081	0.073	0.036
A-13	25	0.377	0.251	0.188	0.151	0.126	0.108	0.094	0.084	0.075	0.038
A-14	30	0.387	0.258	0.194	0.155	0.129	0.111	0.097	0.085	0.077	0.039
A-15	40	0.401	0.268	0.201	0.161	0.134	0.115	0.100	0.089	0.080	0.040
A-16	50	0.412	0.275	0.206	0.165	0.137	0.118	0.103	0.092	0.082	0.041
A-17	75	0.428	0.285	0.214	0.171	0.143	0.122	0.107	0.095	0.086	0.043
A-18	100	0.437	0.291	0.219	0.175	0.146	0.125	0.109	0.097	0.087	0.044

TABLE A1.16 Master Table for Life Tests Terminated at Preassigned Time—Testing With Replacement

NOTE—For explanation of the code, see section 7.3.2 and Table A1.1.

Values of T/θ_0 for $\alpha = 0.25$											
Code	r	Sample Size									
		2r	3r	4r	5r	6r	7r	8r	9r	10r	20r
A-1	1	0.144	0.096	0.072	0.058	0.048	0.041	0.036	0.032	0.029	0.014
A-2	2	0.240	0.160	0.120	0.096	0.080	0.069	0.060	0.053	0.048	0.024
A-3	3	0.288	0.192	0.144	0.115	0.096	0.082	0.071	0.064	0.058	0.029
A-4	4	0.317	0.211	0.158	0.127	0.106	0.091	0.079	0.070	0.061	0.032
A-5	5	0.337	0.225	0.168	0.135	0.112	0.096	0.084	0.075	0.067	0.034
A-6	6	0.352	0.234	0.176	0.141	0.117	0.100	0.088	0.078	0.070	0.035
A-7	7	0.363	0.242	0.182	0.145	0.121	0.104	0.091	0.081	0.073	0.036
A-8	8	0.372	0.248	0.186	0.149	0.124	0.106	0.093	0.083	0.074	0.037
A-9	9	0.380	0.253	0.190	0.152	0.127	0.109	0.095	0.084	0.076	0.038
A-10	10	0.386	0.258	0.193	0.155	0.129	0.110	0.097	0.086	0.077	0.039
A-11	15	0.408	0.271	0.204	0.163	0.136	0.117	0.102	0.091	0.082	0.041
A-12	20	0.421	0.281	0.210	0.168	0.140	0.120	0.105	0.094	0.084	0.042
A-13	25	0.429	0.286	0.215	0.172	0.143	0.123	0.107	0.095	0.086	0.043
A-14	30	0.436	0.291	0.218	0.174	0.145	0.125	0.109	0.097	0.087	0.044
A-15	40	0.445	0.296	0.222	0.178	0.148	0.127	0.111	0.099	0.089	0.044
A-16	50	0.451	0.300	0.225	0.180	0.150	0.129	0.113	0.100	0.090	0.045
A-17	75	0.460	0.307	0.230	0.184	0.153	0.131	0.115	0.102	0.091	0.046
A-18	100	0.465	0.310	0.233	0.186	0.155	0.133	0.116	0.103	0.093	0.047

TABLE A1.17 Master Table for Life Tests Terminated at Preassigned Time—Testing With Replacement

NOTE—For explanation of the code, see section 7.3.2 and Table A1.1.

Values of T/θ_0 for $\alpha = 0.05$

Code	r	Sample Size									
		2r	3r	4r	5r	6r	7r	8r	9r	10r	20r
A-1	1	0.347	0.231	0.173	0.139	0.116	0.099	0.087	0.077	0.069	0.035
A-2	2	0.420	0.280	0.210	0.161	0.140	0.120	0.105	0.093	0.084	0.042
A-3	3	0.446	0.297	0.223	0.178	0.149	0.127	0.111	0.099	0.089	0.045
A-4	4	0.459	0.306	0.230	0.184	0.153	0.131	0.115	0.102	0.092	0.046
A-5	5	0.467	0.311	0.234	0.187	0.156	0.133	0.117	0.104	0.093	0.047
A-6	6	0.473	0.315	0.236	0.189	0.158	0.135	0.118	0.105	0.095	0.047
A-7	7	0.476	0.318	0.238	0.191	0.159	0.136	0.119	0.106	0.095	0.048
A-8	8	0.479	0.320	0.240	0.192	0.160	0.137	0.120	0.107	0.096	0.048
A-9	9	0.482	0.321	0.241	0.193	0.161	0.138	0.120	0.107	0.096	0.048
A-10	10	0.483	0.322	0.242	0.193	0.161	0.138	0.121	0.107	0.097	0.048
A-11	15	0.489	0.326	0.244	0.196	0.163	0.140	0.122	0.109	0.098	0.049
A-12	20	0.492	0.328	0.246	0.197	0.164	0.140	0.123	0.109	0.098	0.049
A-13	25	0.493	0.329	0.247	0.197	0.164	0.141	0.123	0.110	0.099	0.049
A-14	30	0.494	0.330	0.247	0.198	0.165	0.141	0.124	0.110	0.099	0.049
A-15	40	0.496	0.331	0.248	0.198	0.165	0.142	0.124	0.110	0.099	0.050
A-16	50	0.497	0.331	0.248	0.199	0.166	0.142	0.124	0.110	0.099	0.050
A-17	75	0.498	0.332	0.249	0.199	0.166	0.142	0.124	0.111	0.100	0.050
A-18	100	0.498	0.332	0.249	0.199	0.166	0.142	0.125	0.111	0.100	0.050

**TABLE A1.18 Life Tests Terminated at Preassigned Time—Testing Without Replacement
Life Test Sampling Plans for Specified α , β , θ_1/θ_0 and T/θ_0**

NOTE—No operating characteristic curves are provided for these sampling plans. However, two points on the OC curves $(1, 1-\alpha)$ and $(\theta_1/\theta_0, \beta)$ are given.

θ_1/θ_0	r	T/θ_0				r	T/θ_0			
		1/3	1/5	1/10	1/20		1/3	1/5	1/10	1/20
		n	n	n	n		n	n	n	n
		$\alpha = 0.01$		$\beta = 0.01$			$\alpha = 0.05$		$\beta = 0.01$	
2/3	136	403	622	1172	2275	95	289	447	844	1639
1/2	46	119	182	340	657	33	90	138	258	499
1/3	19	41	61	113	216	13	30	45	83	160
1/5	9	15	22	39	74	7	13	20	36	69
1/10	5	6	9	15	28	4	6	9	15	29
		$\alpha = 0.01$		$\beta = 0.05$			$\alpha = 0.05$		$\beta = 0.05$	
2/3	101	291	448	842	1633	67	198	305	575	1116
1/2	35	87	132	245	472	23	59	90	168	326
1/3	15	30	45	82	157	10	21	32	59	113
1/5	8	13	18	33	62	5	8	12	22	41
1/10	4	4	6	10	18	3	4	5	9	17
		$\alpha = 0.01$		$\beta = 0.10$			$\alpha = 0.05$		$\beta = 0.10$	
2/3	83	234	359	675	1307	55	159	245	462	895
1/2	30	72	109	202	390	19	47	72	134	258
1/3	13	25	37	67	128	8	16	24	43	83
1/5	7	11	15	26	50	4	6	9	15	29
1/10	4	4	6	10	18	3	4	5	9	17
		$\alpha = 0.01$		$\beta = 0.10$			$\alpha = 0.05$		$\beta = 0.10$	
2/3	60	162	248	465	899	35	96	147	276	535
1/2	22	49	74	137	262	13	30	45	83	160
1/3	10	18	26	46	87	6	11	16	29	55
1/5	5	6	9	15	28	3	4	5	9	17
1/10	3	3	4	6	10	2	2	2	4	8
		$\alpha = 0.10$		$\beta = 0.01$			$\alpha = 0.25$		$\beta = 0.01$	
2/3	77	238	369	699	1358	52	168	261	496	965
1/2	26	73	112	210	407	17	51	79	149	289
1/3	11	27	40	75	145	7	19	29	54	105
1/5	5	10	14	26	51	3	6	10	18	36
1/10	3	5	7	12	23	2	3	5	10	29
		$\alpha = 0.10$		$\beta = 0.05$			$\alpha = 0.25$		$\beta = 0.05$	
2/3	52	156	242	456	886	32	101	156	296	576
1/2	18	48	73	137	265	11	31	48	91	177
1/3	8	18	27	50	97	5	12	19	36	69
1/5	4	7	10	19	36	2	3	5	10	20
1/10	2	2	3	6	11	2	3	5	10	20
		$\alpha = 0.10$		$\beta = 0.10$			$\alpha = 0.25$		$\beta = 0.10$	
2/3	41	121	186	351	681	23	71	109	207	403
1/2	15	39	59	110	213	8	22	33	63	123
1/3	6	12	18	34	66	4	9	14	27	52
1/5	3	5	7	12	23	2	3	5	10	20
1/10	2	2	3	6	11	1	1	1	3	6
		$\alpha = 0.10$		$\beta = 0.25$			$\alpha = 0.25$		$\beta = 0.25$	
2/3	25	69	107	201	389	12	34	53	101	196
1/2	9	21	31	58	113	5	12	19	36	69
1/3	4	7	10	19	36	2	3	5	10	20
1/5	3	5	7	12	23	1	1	1	3	6
1/10	2	2	3	6	11	1	1	1	3	6

TABLE A1.19 Life Tests Terminated at Preassigned Time—Testing With Replacement
Life Test Sampling Plans for Specified α , β , θ_1/θ_0 and T/θ_0

NOTE—No operating characteristic curves are provided for these sampling plans. However, two points on the OC curves $(1, 1-\alpha)$ and $(\theta_1/\theta_0, \beta)$ are given.

θ_1/θ_0	r	T/θ_0				r	T/θ_0			
		1/3	1/5	1/10	1/20		1/3	1/5	1/10	1/20
		n	n	n	n		n	n	n	n
		$\alpha = 0.01$		$\beta = 0.01$			$\alpha = 0.05$		$\beta = 0.01$	
2/3	136	331	551	1103	2206	95	238	397	795	1591
1/2	46	95	158	317	634	33	72	120	241	483
1/3	19	31	51	103	206	13	23	38	76	153
1/5	9	10	17	35	70	7	9	16	32	65
1/10	5	3	6	12	25	4	4	6	13	27
		$\alpha = 0.01$		$\beta = 0.05$			$\alpha = 0.05$		$\beta = 0.05$	
2/3	101	237	395	790	1581	67	162	270	541	1082
1/2	35	68	113	227	454	23	47	78	157	314
1/3	15	22	37	74	149	10	16	27	54	108
1/5	8	8	14	29	58	5	5	9	19	39
1/10	4	2	4	8	16	3	2	4	8	16
		$\alpha = 0.01$		$\beta = 0.10$			$\alpha = 0.05$		$\beta = 0.10$	
2/3	83	189	316	632	1265	55	130	216	433	867
1/2	30	56	93	187	374	19	37	62	124	248
1/3	13	18	30	60	121	8	11	19	39	79
1/5	7	6	11	23	46	4	4	6	13	27
1/10	4	2	4	8	16	3	2	4	8	16
		$\alpha = 0.01$		$\beta = 0.10$			$\alpha = 0.05$		$\beta = 0.10$	
2/3	60	130	217	434	869	35	77	129	258	517
1/2	22	37	62	125	251	13	23	38	76	153
1/3	10	12	20	41	82	6	7	13	26	52
1/5	5	3	6	12	25	3	2	4	8	16
1/10	3	1	2	4	8	2	1	1	3	7
		$\alpha = 0.10$		$\beta = 0.01$			$\alpha = 0.25$		$\beta = 0.01$	
2/3	77	197	329	659	1319	52	140	234	469	939
1/2	26	59	98	197	394	17	42	70	140	281
1/3	11	21	35	70	140	7	15	25	50	101
1/5	5	7	12	24	48	3	5	8	17	34
1/10	3	3	5	11	22	2	2	4	9	19
		$\alpha = 0.10$		$\beta = 0.05$			$\alpha = 0.25$		$\beta = 0.05$	
2/3	52	128	214	429	859	32	84	140	280	560
1/2	18	38	64	128	256	11	25	43	86	172
1/3	8	13	23	46	93	5	10	16	33	67
1/5	4	5	8	17	34	2	2	4	9	19
1/10	2	1	2	5	10	2	2	4	9	19
		$\alpha = 0.10$		$\beta = 0.10$			$\alpha = 0.25$		$\beta = 0.10$	
2/3	41	99	165	330	660	23	58	98	196	392
1/2	15	30	51	102	205	8	17	29	59	119
1/3	6	9	15	31	63	4	7	12	25	50
1/5	3	3	5	11	22	2	2	4	9	19
1/10	2	1	2	5	10	1	0	1	2	5
		$\alpha = 0.10$		$\beta = 0.25$			$\alpha = 0.25$		$\beta = 0.25$	
2/3	25	56	94	188	376	12	28	47	95	190
1/2	9	16	27	54	108	5	10	16	33	67
1/3	4	5	8	17	34	2	2	4	9	19
1/5	3	3	5	11	22	1	0	1	2	5
1/10	2	1	2	5	10	1	0	1	2	5

TABLE A1.20 Life Tests Terminated at Preassigned Time—Testing Without Replacement
Life Test Sampling Plans for Specified α , β , and p_1/p_0

Values of r (upper numbers) and of D (lower numbers) ^A									
p_1/p_0	$\alpha = 0.01$			$\alpha = 0.05$			$\alpha = 0.10$		
	$\beta = 0.01$	0.05	0.1	0.01	0.05	0.1	0.01	0.05	0.1
1½	136.00	101.00	83.00	95.00	67.00	55.00	77.00	52.00	41.00
2	110.40	79.10	63.30	79.60	54.10	43.40	66.00	43.00	33.00
	46.00	35.00	30.00	33.00	23.00	19.00	26.00	18.00	15.00
	31.70	22.70	18.70	24.20	15.70	12.40	19.70	12.80	10.30
2½	27.00	21.00	18.00	19.00	14.00	11.00	15.00	11.00	9.00
3	16.40	11.80	9.62	12.40	8.46	6.17	10.30	7.02	5.43
	19.00	15.00	13.00	13.00	10.00	8.00	11.00	8.00	6.00
	10.30	7.48	6.10	7.69	5.43	3.98	7.02	4.66	3.15
4	12.00	10.00	9.00	9.00	7.00	6.00	7.00	5.00	4.00
5	5.43	4.13	3.51	4.70	3.29	2.61	3.90	2.43	1.75
	9.00	8.00	7.00	7.00	5.00	4.00	5.00	4.00	3.00
	3.51	2.91	2.33	3.29	1.97	1.37	2.43	1.75	1.10
10	5.00	4.00	4.00	4.00	3.00	3.00	3.00	2.00	2.00
	1.28	0.823	0.823	1.37	0.818	0.818	1.10	0.532	0.532

^A The sample size n is obtained by taking the largest integer less than or equal to the tabled value divided by p_0 , i.e., $n = [D/p_0]$. Producer's risk α is the probability of rejecting lots with acceptable proportion of lot failing before specified time, p_0 . Consumer's risk β is the probability of accepting lots with unacceptable proportion of lot failing before specified time, p_1 .

EXAMPLE OF SEQUENTIAL LIFE TEST

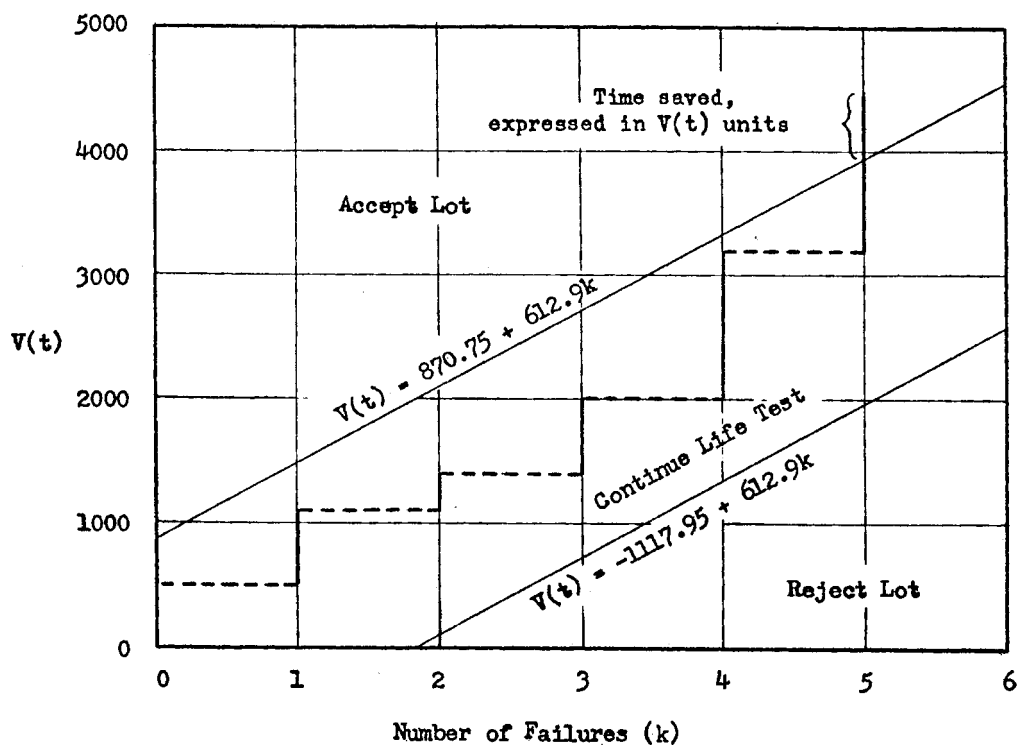


FIG. A1.2 Example of Sequential Life Test

EXAMPLE OF TRUNCATED SEQUENTIAL LIFE TEST

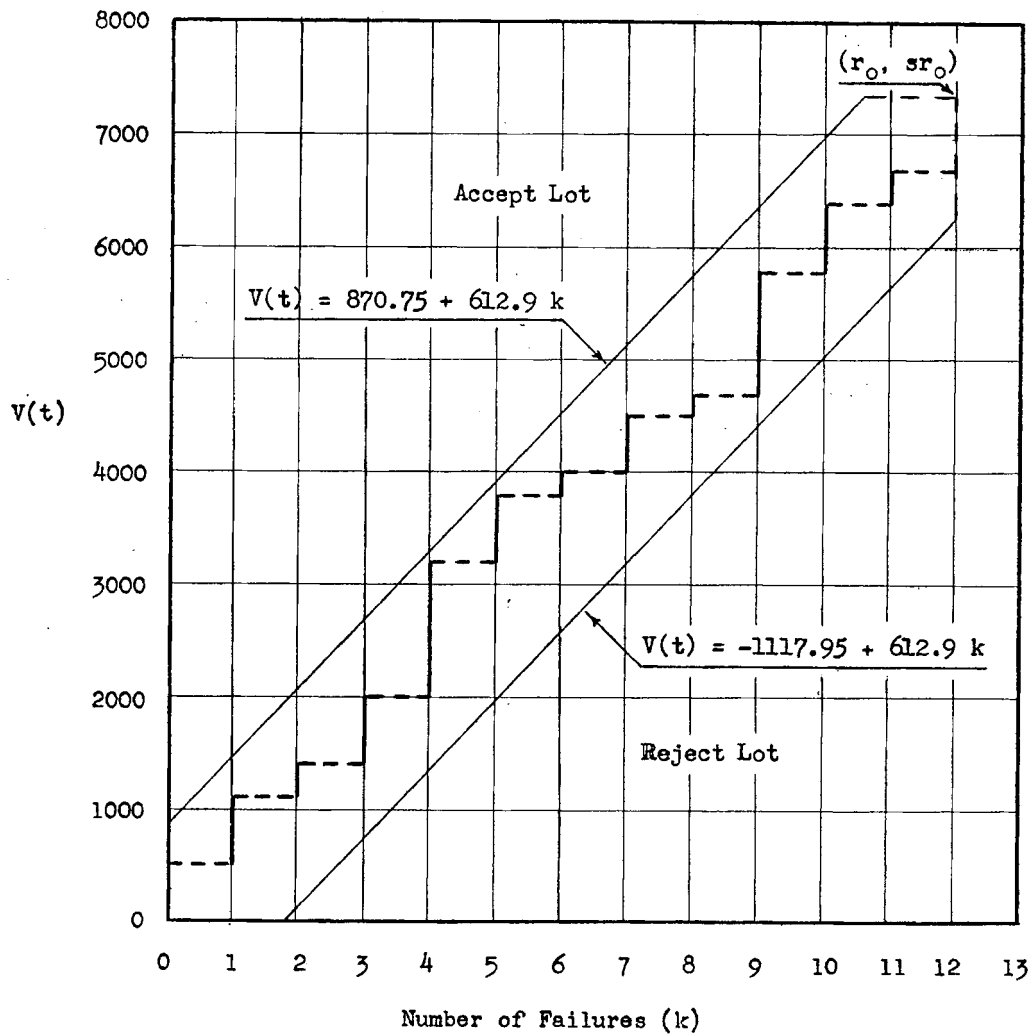


FIG. A1.3 Example of Truncated Sequential Life Test

TABLE A1.21 Master Table for Sequential Life Tests

NOTE—For explanation of the code, see section 7.3.2 and Table A1.1.

$\alpha = 0.01$								
Code	r_o	h_o/θ_o	h_1/θ_o	s/θ_o	$E_o(r)$	$E_{o1}(r)$	$E_s(r)$	$E_{o0}(r)$
A-1	3	0.0092	-0.0181	0.0222	0.8	0.8	0.3	0.0
A-2	6	0.0906	-0.1777	0.1292	1.4	1.7	1.0	0.1
A-3	9	0.2048	-0.4019	0.2234	1.8	2.4	1.6	0.3
A-4	12	0.3215	-0.6311	0.2939	2.1	3.1	2.3	0.4
A-5	15	0.4367	-0.8571	0.3491	2.5	3.8	3.1	0.7
A-6	18	0.5483	-1.0762	0.3934	2.7	4.6	3.8	0.9
A-7	21	0.6504	-1.2766	0.4283	3.0	5.2	4.5	1.1
A-8	24	0.7520	-1.4760	0.4587	3.2	5.9	5.3	1.3
A-9	27	0.8479	-1.6643	0.4843	3.4	6.6	6.0	1.6
A-10	30	0.9409	-1.8469	0.5067	3.6	7.3	6.8	1.9
A-11	45	1.3522	-2.6541	0.5848	4.5	10.5	10.5	3.2
A-12	60	1.7154	-3.3670	0.6350	5.3	13.8	14.3	4.6
A-13	75	2.0330	-3.9904	0.6695	6.0	17.0	18.1	6.0
A-14	90	2.3295	-4.5724	0.6962	6.6	20.2	22.0	7.4
A-15	120	2.8477	-5.5894	0.7336	7.6	26.4	29.6	10.4
A-16	150	3.3127	-6.5022	0.7600	8.6	32.7	37.3	13.4
A-17	225	4.3142	-8.4679	0.8020	10.6	48.3	56.8	21.1
A-18	300	5.1508	-10.1100	0.8272	12.2	63.5	76.1	28.9

TABLE A1.22 Master Table for Sequential Life Tests

NOTE—For explanation of the code, see section 7.3.2 and Table A1.1.

$\alpha = 0.05$								
Code	r_0	h_0/θ_0	h_1/θ_0	s/θ_0	$E_0(r)$	$E_{01}(r)$	$E_s(r)$	$E_{00}(r)$
B-1	3	0.0506	-0.0650	0.0859	0.8	0.8	0.4	0.0
B-2	6	0.2254	-0.2894	0.2400	1.2	1.6	1.1	0.3
B-3	9	0.4098	-0.5261	0.3405	1.5	2.3	1.9	0.6
B-4	12	0.5805	-0.7453	0.4086	1.8	3.0	2.6	0.9
B-5	15	0.7345	-0.9430	0.4576	2.1	3.7	3.3	1.2
B-6	18	0.8842	-1.1352	0.4972	2.3	4.3	4.1	1.6
B-7	21	1.0209	-1.3107	0.5282	2.5	5.0	4.8	1.9
B-8	24	1.1495	-1.4757	0.5538	2.7	5.6	5.5	2.3
B-9	27	1.2719	-1.6329	0.5756	2.8	6.3	6.3	2.7
B-10	30	1.3916	-1.7866	0.5948	3.0	6.9	7.0	3.0
B-11	45	1.9101	-2.4523	0.6607	3.7	10.0	10.7	5.0
B-12	60	2.3620	-3.0325	0.7024	4.3	13.1	14.5	7.0
B-13	75	2.7516	-3.5327	0.7307	4.8	16.1	18.2	9.1
B-14	90	3.1217	-4.0079	0.7529	5.3	19.2	22.1	11.2
B-15	120	3.7522	-4.8173	0.7833	6.1	25.0	29.5	15.3
B-16	150	4.3314	-5.5610	0.8053	6.9	31.0	37.1	19.7
B-17	225	5.5386	-7.1109	0.8391	8.5	45.6	55.9	30.5
B-18	300	6.5773	-8.4444	0.8600	9.8	60.4	75.1	41.6

TABLE A1.23 Master Table for Sequential Life Tests

NOTE—For explanation of the code, see section 7.3.2 and Table A1.1.

$\alpha = 0.10$								
Code	r_0	h_0/θ_0	h_1/θ_0	s/θ_0	$E_0(r)$	$E_{01}(r)$	$E_s(r)$	$E_{00}(r)$
C-1	3	0.1059	-0.1059	0.1485	0.7	0.8	0.5	0.1
C-2	6	0.3488	-0.3488	0.3156	1.1	1.6	1.2	0.4
C-3	9	0.5736	-0.5736	0.4111	1.4	2.2	1.9	0.8
C-4	12	0.7760	-0.7760	0.4744	1.6	2.9	2.7	1.2
C-5	15	0.9597	-0.9597	0.5201	1.8	3.6	3.4	1.6
C-6	18	1.1319	-1.1319	0.5558	2.0	4.2	4.1	2.0
C-7	21	1.2904	-1.2904	0.5839	2.2	4.8	4.9	2.5
C-8	24	1.4406	-1.4406	0.6073	2.4	5.5	5.6	2.5
C-9	27	1.5781	-1.5781	0.6265	2.5	6.1	6.3	3.4
C-10	30	1.7124	-1.7124	0.6434	2.7	6.7	7.1	3.8
C-11	45	2.3053	-2.3053	0.7024	3.3	9.7	10.8	6.2
C-12	60	2.8078	-2.8078	0.7387	3.8	12.6	14.4	8.6
C-13	75	3.2549	-3.2549	0.7642	4.3	15.6	18.1	11.0
C-14	90	3.6465	-3.6465	0.7827	4.7	18.4	21.7	13.4
C-15	120	4.3813	-4.3813	0.8105	5.4	24.3	29.2	18.5
C-16	150	5.0068	-5.0068	0.8291	6.0	29.9	36.5	23.4
C-17	225	6.3523	-6.3523	0.8588	7.4	43.9	54.7	36.0
C-18	300	7.5250	-7.5250	0.8774	8.6	58.2	73.6	49.1

TABLE A1.24 Master Table for Sequential Life Tests

NOTE—For explanation of the code, see section 7.3.2 and Table A1.1.

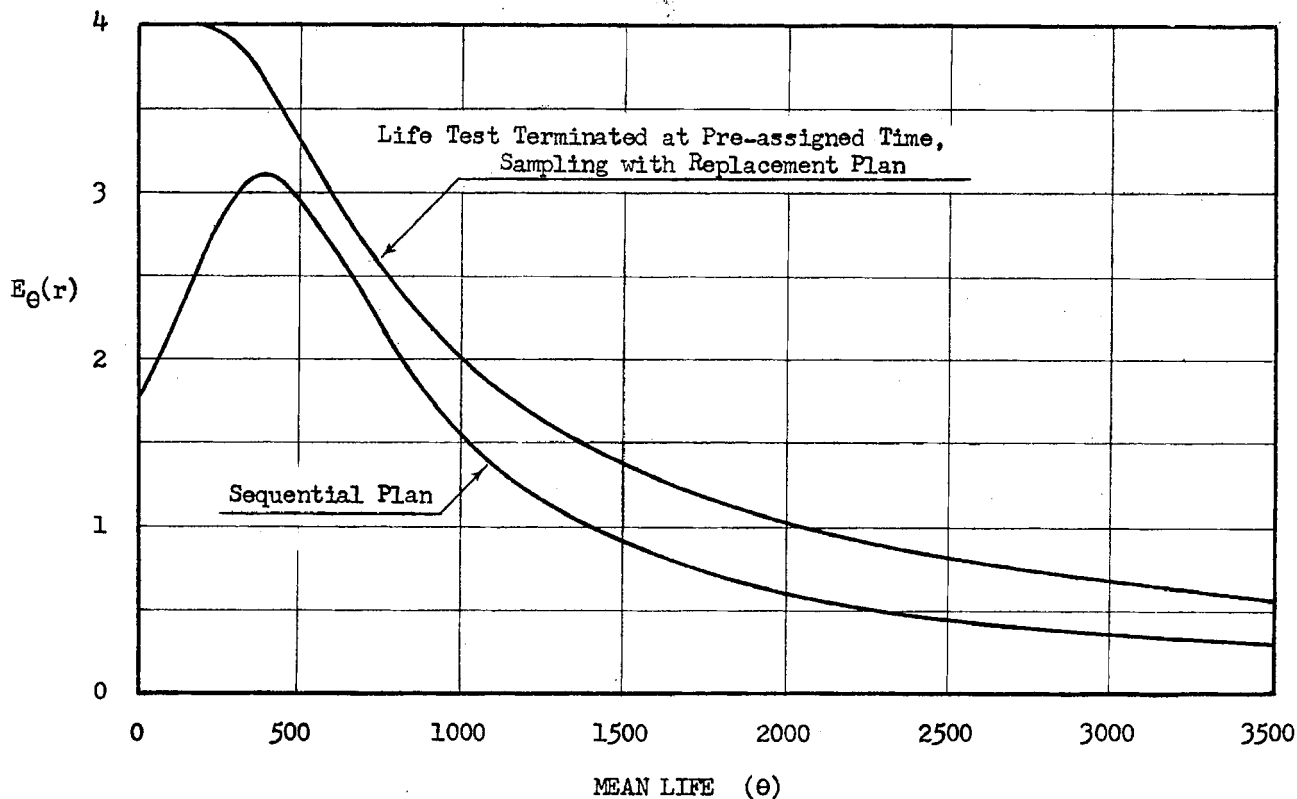
$\alpha = 0.25$								
Code	r_0	h_0/θ_0	h_1/θ_0	s/θ_0	$E_0(r)$	$E_{01}(r)$	$E_s(r)$	$E_{00}(r)$
D-1	3	0.2878	-0.1830	0.2971	0.6	0.8	0.6	0.2
D-2	6	0.6609	-0.4202	0.4587	0.9	1.5	1.3	0.7
D-3	9	0.9701	-0.6167	0.5412	1.1	2.1	2.0	1.2
D-4	12	1.2297	-0.7818	0.3921	1.3	2.7	2.7	1.8
D-5	15	1.4651	-0.9314	0.6290	1.5	3.3	3.4	2.3
D-6	18	1.6822	-1.0694	0.6574	1.6	3.9	4.2	2.9
D-7	21	1.8824	-1.1967	0.6799	1.8	4.5	4.5	3.5
D-8	24	2.0638	-1.3120	0.6978	1.9	5.1	5.6	4.0
D-9	27	2.2359	-1.4215	0.7129	2.0	5.6	6.3	4.6
D-10	30	2.4037	-1.5281	0.7263	2.1	6.2	7.0	5.2
D-11	45	3.1252	-1.9868	0.7718	2.6	9.0	10.4	8.1
D-12	60	3.7420	-2.3789	0.8000	3.0	11.8	13.5	11.1
D-13	75	4.2817	-2.7220	0.8195	3.3	14.5	17.4	14.0
D-14	90	4.7693	-3.0320	0.8341	3.6	17.2	20.8	17.0
D-15	120	5.6463	-3.3895	0.8552	4.2	22.6	27.7	23.0
D-16	150	6.4157	-4.0786	0.8696	4.7	27.9	34.6	29.1
D-17	225	8.0596	-5.1237	0.8926	5.7	41.1	51.8	44.3
D-18	300	9.4334	-5.9971	0.9063	6.6	54.1	68.9	59.5

TABLE A1.25 Master Table for Sequential Life Tests

NOTE—For explanation of the code, see section 7.3.2 and Table A1.1.

$\alpha = 0.50$								
Code	r_0	h_0/θ_0	h_1/θ_0	s/θ_0	$E_0(r)$	$E_{01}(r)$	$E_s(r)$	$E_{00}(r)$
E-1	3	0.6910	-0.2531	0.5170	0.5	0.7	0.7	0.5
E-2	6	1.2241	-0.4470	0.6384	0.7	1.4	1.3	1.1
E-3	9	1.6224	-0.5925	0.6947	0.9	1.9	2.0	1.7
E-4	12	1.9671	-0.7184	0.7307	1.0	2.5	2.6	2.3
E-5	15	2.1594	-0.8252	0.7551	1.1	3.0	3.3	2.9
E-6	18	2.5279	-0.9232	0.7738	1.2	3.6	3.9	3.5
E-7	21	2.7760	-1.0138	0.7887	1.3	4.1	4.5	4.2
E-8	24	3.0154	-1.1013	0.8013	1.4	4.6	5.2	4.8
E-9	27	3.2237	-1.1773	0.8111	1.5	5.1	5.8	5.4
E-10	30	3.4358	-1.2548	0.8202	1.5	5.6	6.4	6.1
E-11	45	4.3294	-1.5812	0.8503	1.9	8.2	9.5	9.2
E-12	60	5.0687	-1.8512	0.8685	2.1	10.6	12.4	12.2
E-13	75	5.7396	-2.0962	0.8815	2.4	13.1	15.5	15.4
E-14	90	6.3581	-2.3220	0.8914	2.6	15.6	18.6	18.6
E-15	120	7.3818	-2.6959	0.9046	3.0	20.2	24.3	24.6
E-16	150	8.3254	-3.0405	0.9142	3.3	25.0	30.3	30.8
E-17	225	10.3123	-3.7662	0.9292	4.1	36.7	45.0	46.3
E-18	300	12.0299	-4.3935	0.9315	4.7	48.7	60.0	62.1

COMPARISON OF EXPECTED NUMBER OF FAILURES REQUIRED FOR DECISION FOR SEQUENTIAL AND LIFE TEST TERMINATED AT PRE-ASSIGNED TIME, SAMPLING WITH REPLACEMENT PLANS

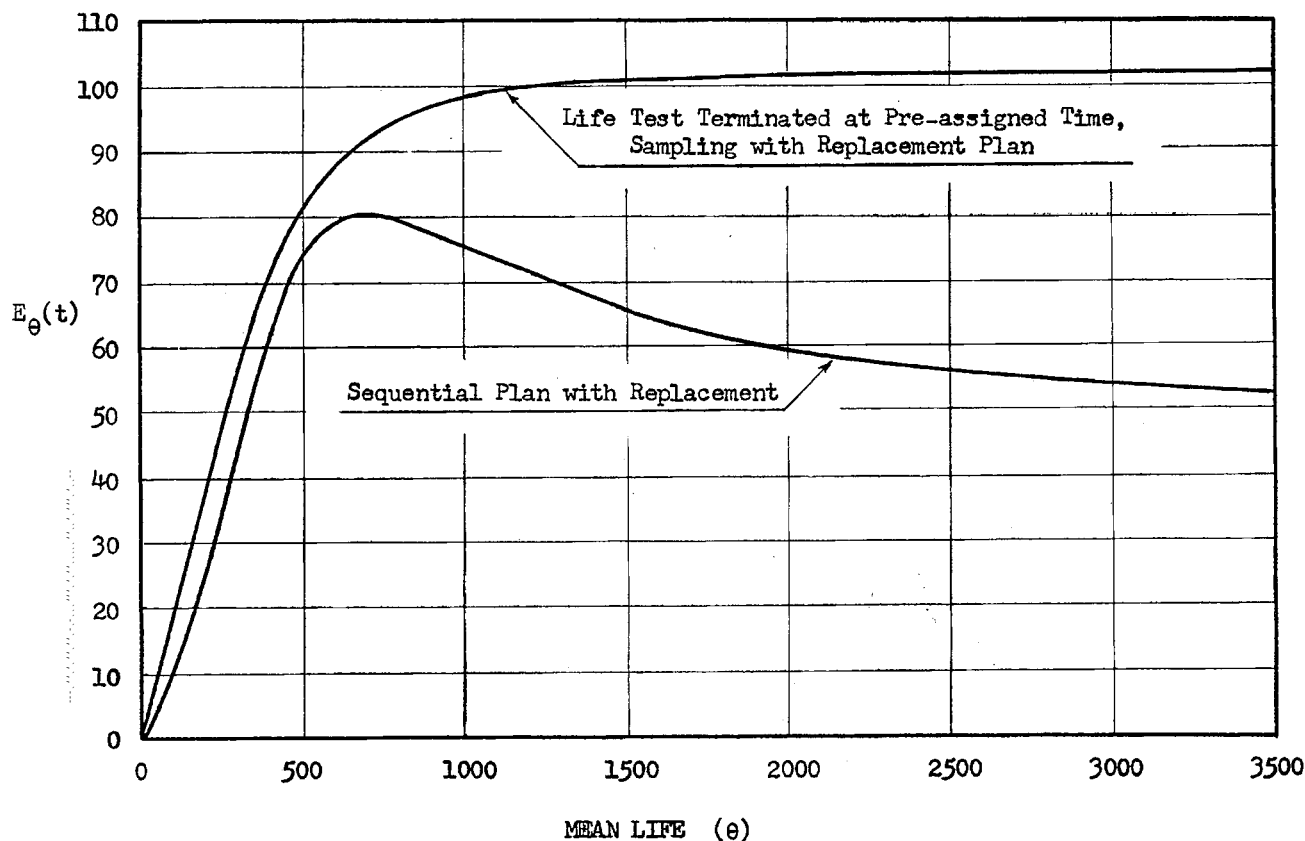


The OC curve for each plan is such that $\theta_0 = 1500$, $\theta_1 = 300$, $\alpha = 0.05$, and $\beta = 0.10$.

NOTE—The OC curve for each plan is such that $\theta_0 = 1500$, $\theta_1 = 300$, $\alpha = 0.05$, and $\beta = 0.10$

FIG. A1.4 Comparison of Expected Number of Failures Required for Decision for Sequential and Life Test Terminated at Preassigned Time, Sampling With Replacement Plans

COMPARISON OF EXPECTED WAITING TIME REQUIRED FOR DECISION FOR SEQUENTIAL AND LIFE TEST TERMINATED AT PRE-ASSIGNED TIME, SAMPLING WITH REPLACEMENT PLANS



The OC curve for each plan is such that $\theta_0 = 1500$, $\theta_1 = 300$, $\alpha = 0.05$, and $\beta = 0.10$.

NOTE—The OC curve for each plan is such that $\theta_0 = 1500$, $\theta_1 = 300$, $\alpha = 0.05$, and $\beta = 0.10$

FIG. A1.5 Comparison of Expected Waiting Time Required for Decision for Sequential and Life Test Terminated at Preassigned Time, Sampling With Replacement Plans

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